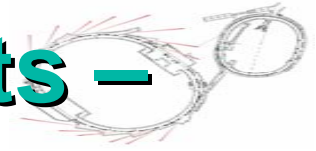


# Storage ring measurements – the basics



## ○ Beam Diagnostics

↪ DCCT

↪ BPMs

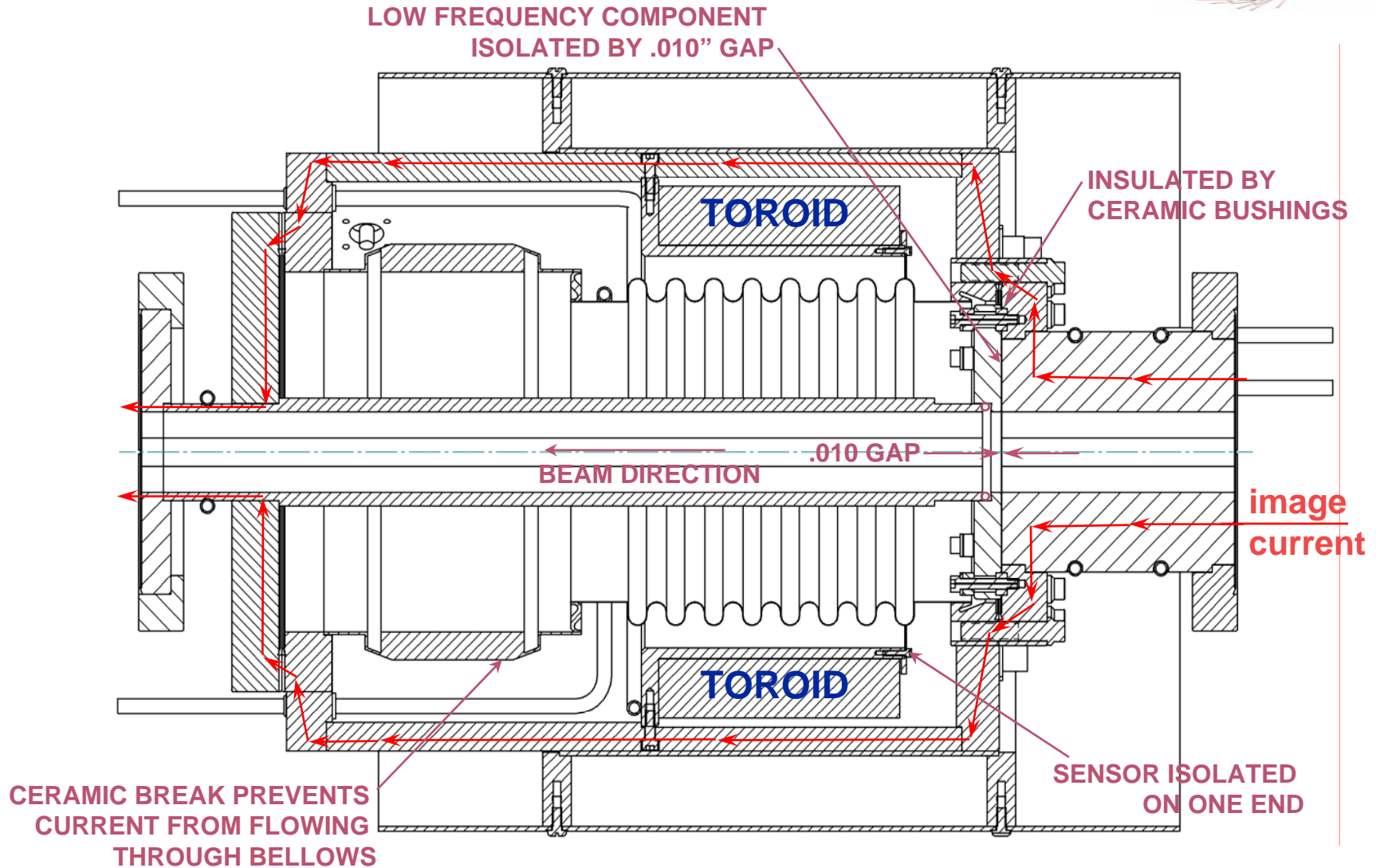
↪ Synchrotron light monitors

↪ Scrapers

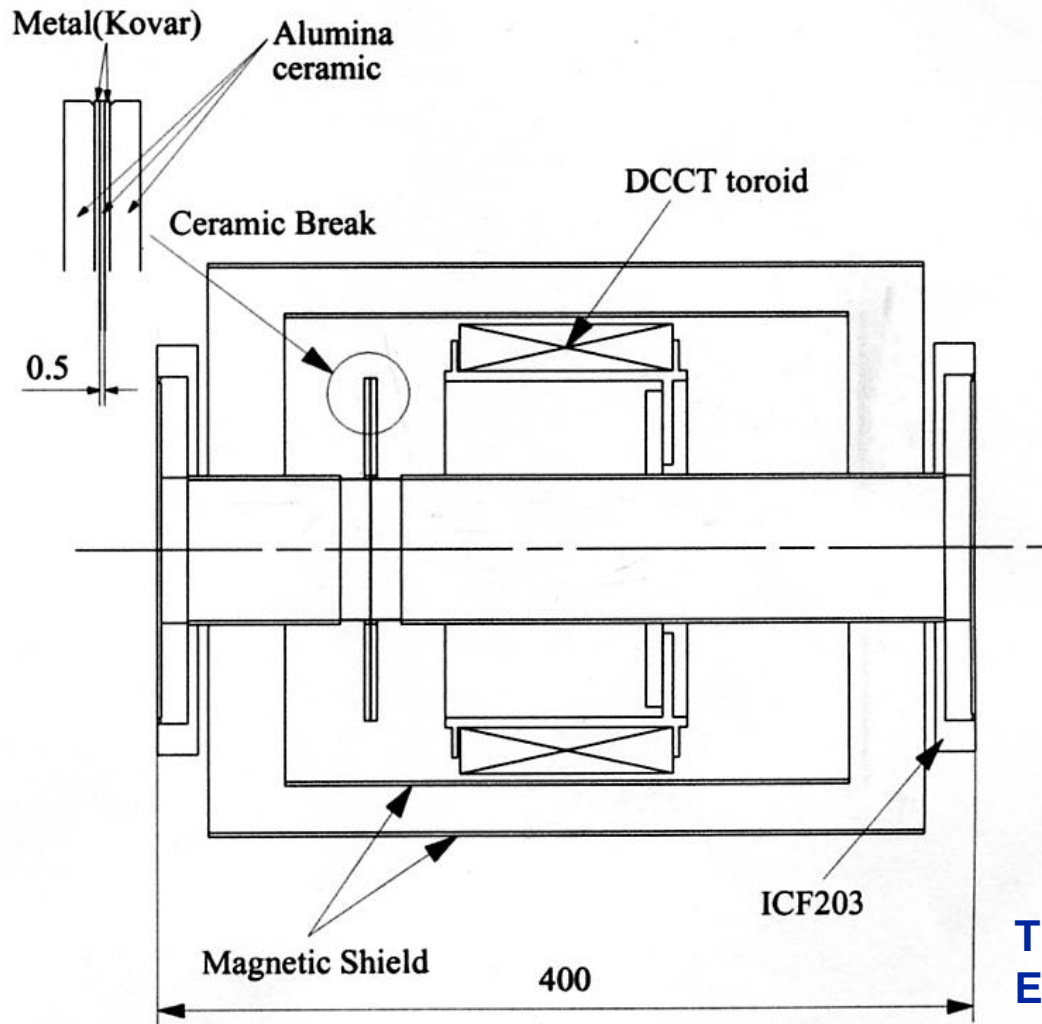
↪ Loss monitors

## ○ Measuring tunes, $\beta$ , $\eta$ , chromaticity, $\alpha$

# SPEAR3 DCCT

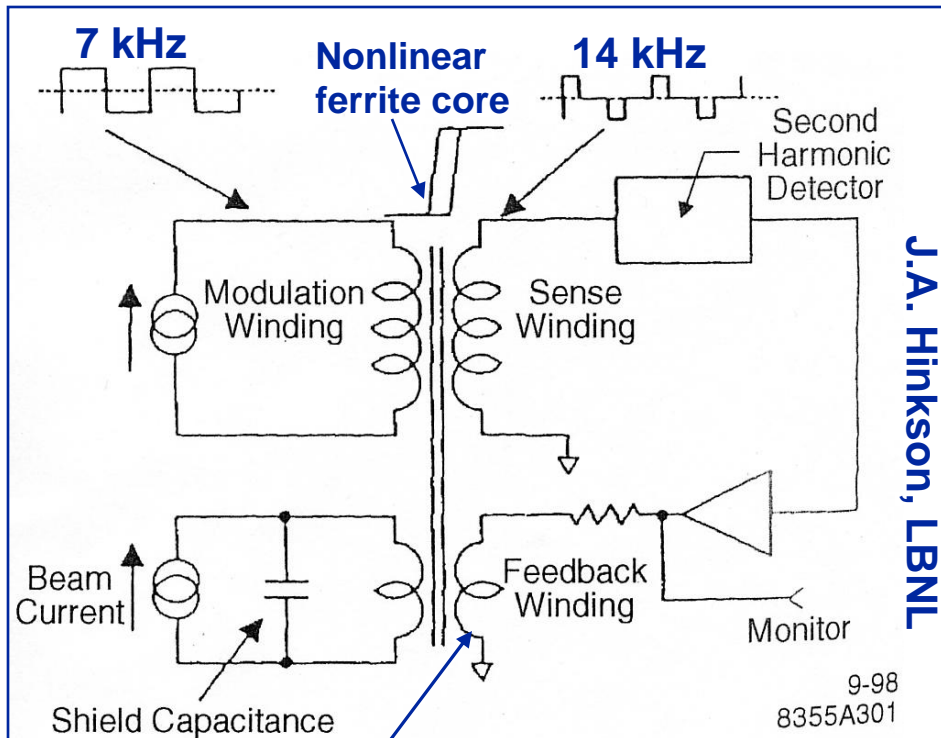


# Photon factory DCCT



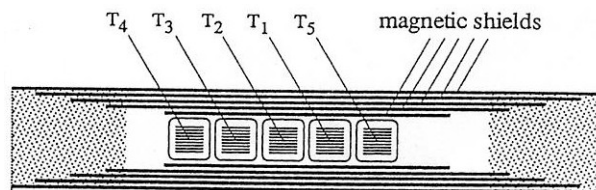
T. Honda et al.,  
EPAC98

# DCCT (or PCT) circuit

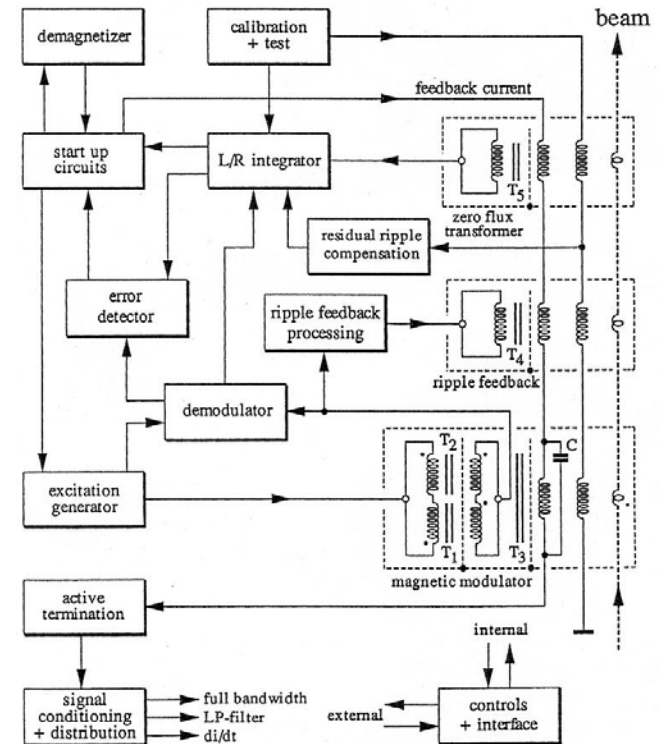


The DC bias current is adjusted to remove the 2<sup>nd</sup> harmonic (14 kHz) response of toroid. The beam current is proportional to the DC bias current.

Ferrite core Xsection



## Bergoz PCT

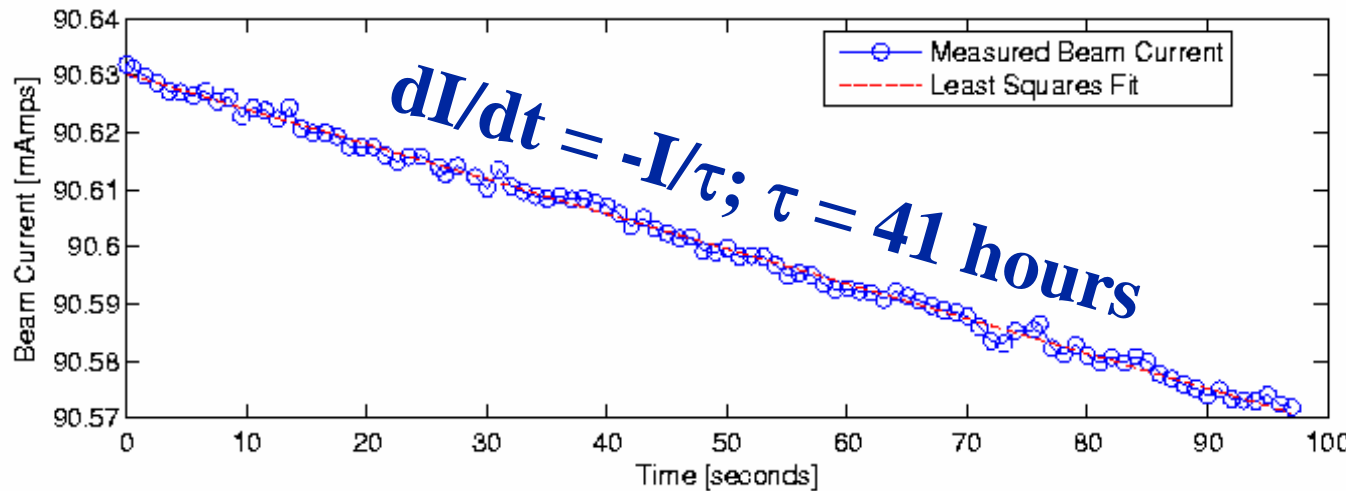


Simplified circuit, K. Unser, 1992

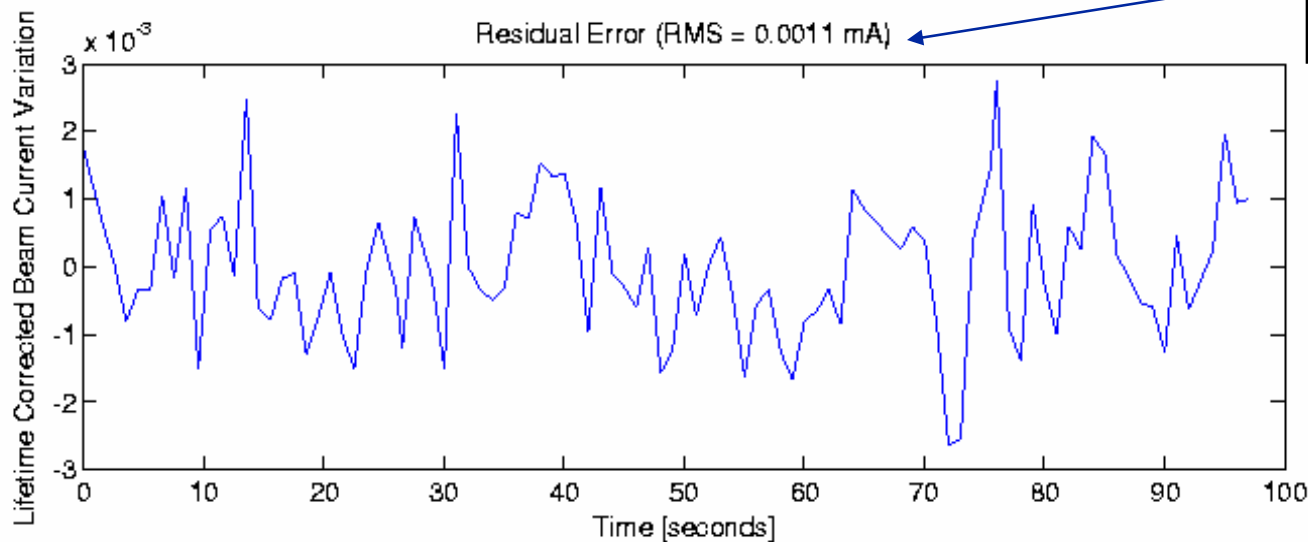
# SPEAR3 lifetime measurement w/ DCCT



Beam Current vs Time: Lifetime=41.17 hours.



DCCT resolution:  
1  $\mu$ A in 1 second



11-Feb-2005

# Lifetime vs. tunes

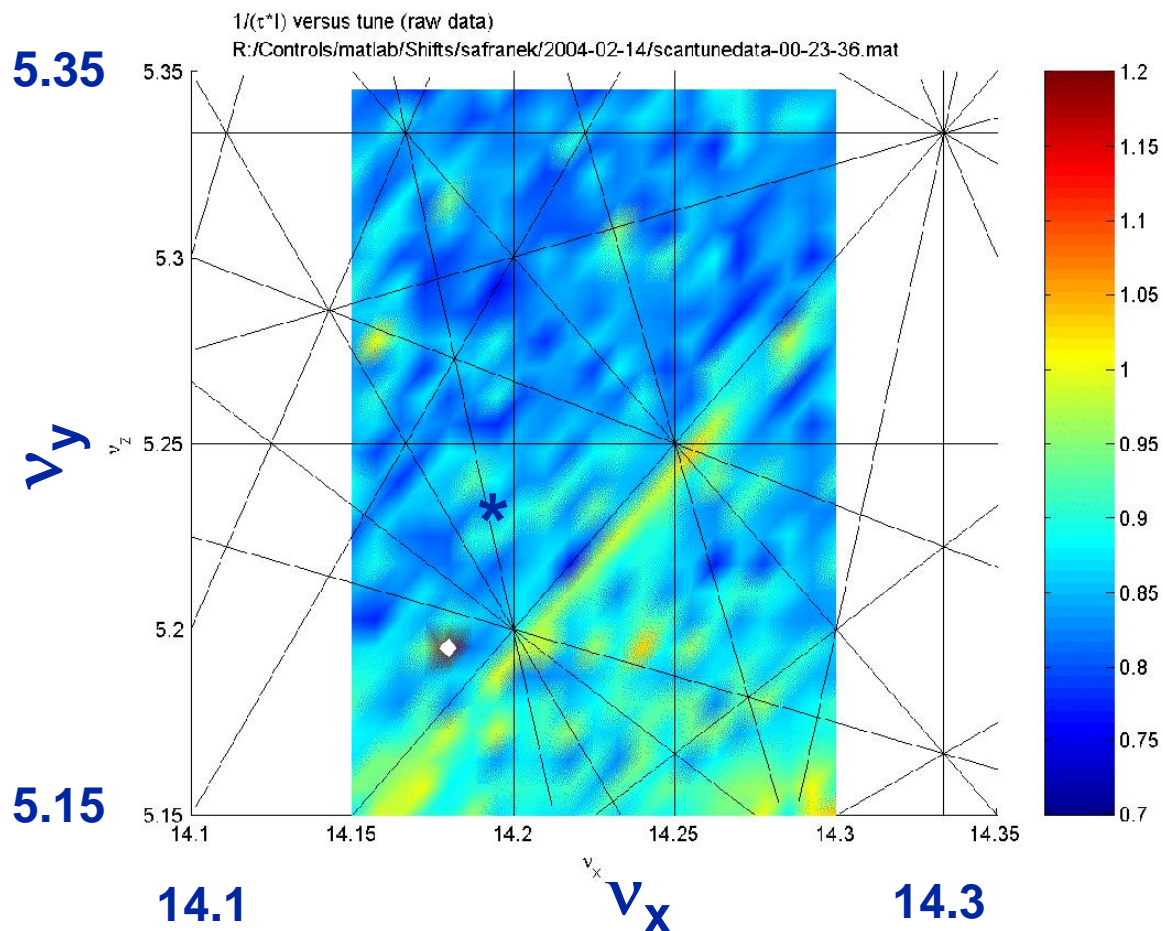


- Resonant line:

$$\leftarrow \nu_x - \nu_y = 9$$

- \* = operating tunes (14.19, 5.23)

- Data gathered automatically on owl shift.



# Dynamic aperture vs. tune



## ○ Resonant lines:

↖  $v_x - v_y = 9$

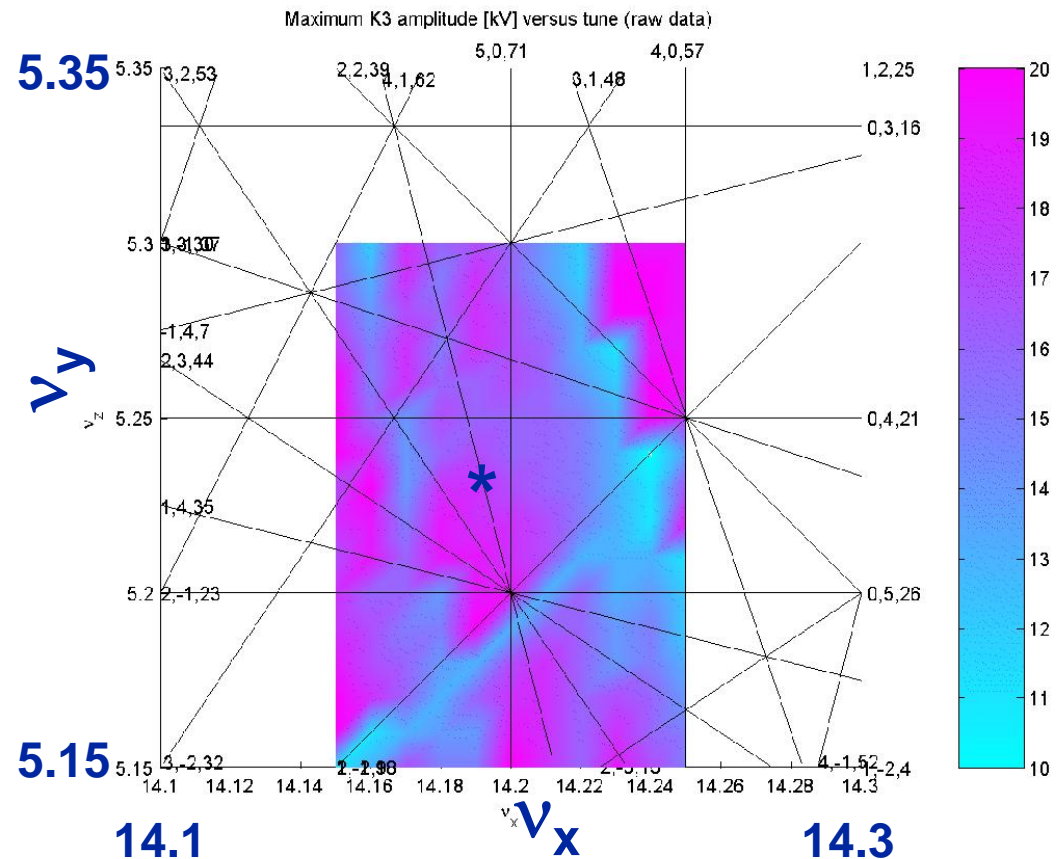
↖  $3v_x + v_y = 48$

↖  $4v_x + v_y = 62$

## ○ Resonances offset from tune shift with amplitude.

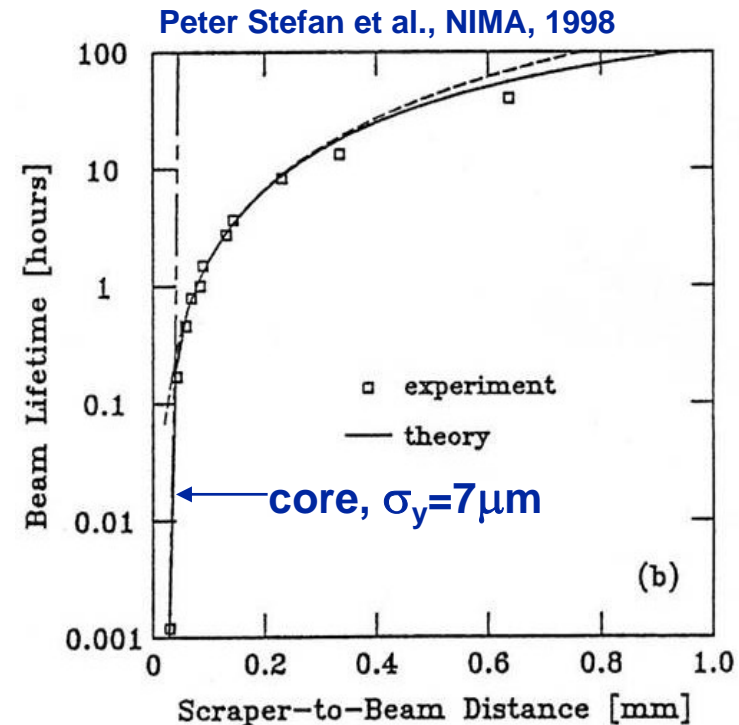
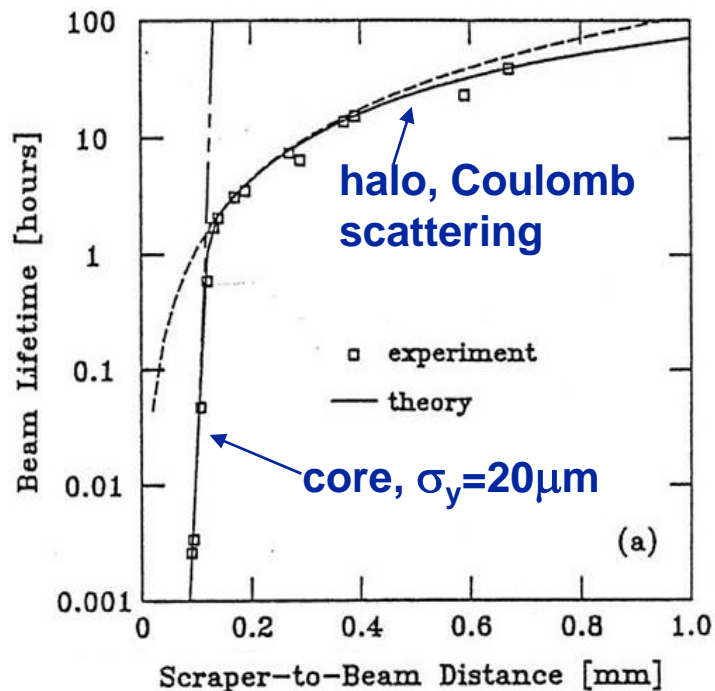
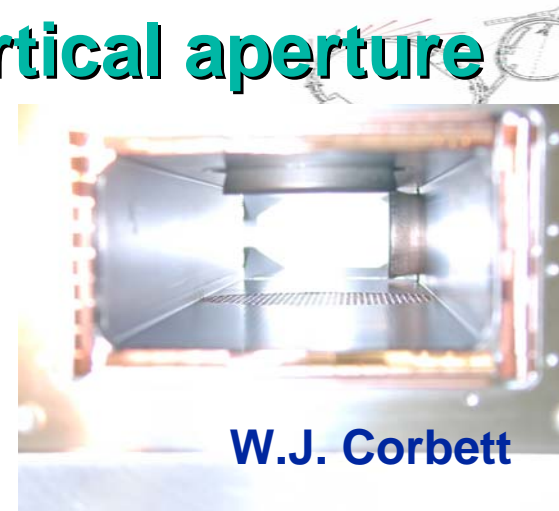
## ○ \* = operating tunes (14.19, 5.23)

## ○ Data gathered automatically on owl shift.



# Beam scrapers; lifetime vs. vertical aperture

Scrapers measure beam halo





# SPEAR3 scraper measurements

Three contributions to lifetime:

- Elastic gas scattering (Coulomb)
- Bremsstrahlung
- Intrabeam scattering (Touschek)

$$\frac{1}{\tau} = \frac{1}{\tau_C} + \frac{1}{\tau_B} + \frac{1}{\tau_T}$$

Five fit parameters:

$$\tau_{C0}, \tau_{B0}, \tau_{T0},$$

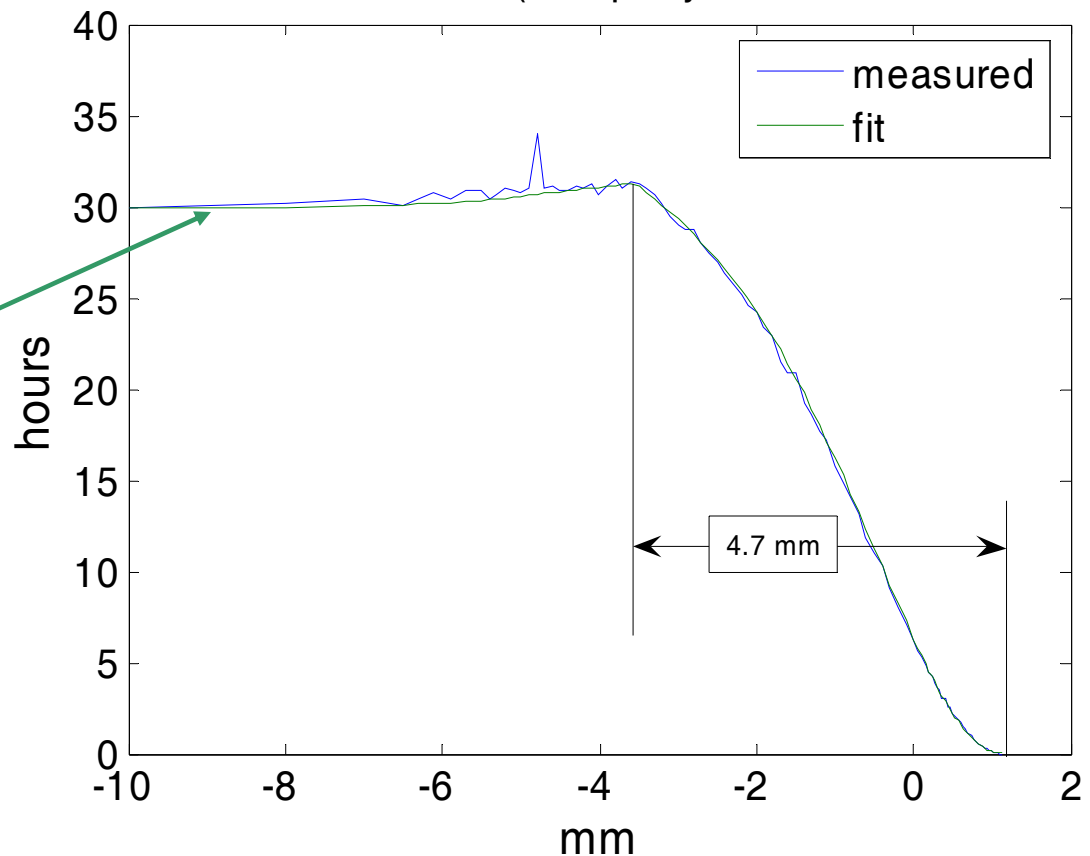
$$y_{beam}, y_{ring}$$

$$\tau_C \propto \text{pressure} * y_{\text{aperture}}^2 \approx I_{\text{tot}} * y^2$$

$$\tau_B \propto \text{pressure} * f(E_{\text{aperture}}) \approx I_{\text{tot}}$$

$$\tau_T \propto \frac{I_{\text{tot}}}{N_{\text{bunch}}} * f(E_{\text{aperture}}) \approx I_b$$

~100 mA, 280 bunches (Scraper y 2005-02-02 00-43-19)



Basic measurements

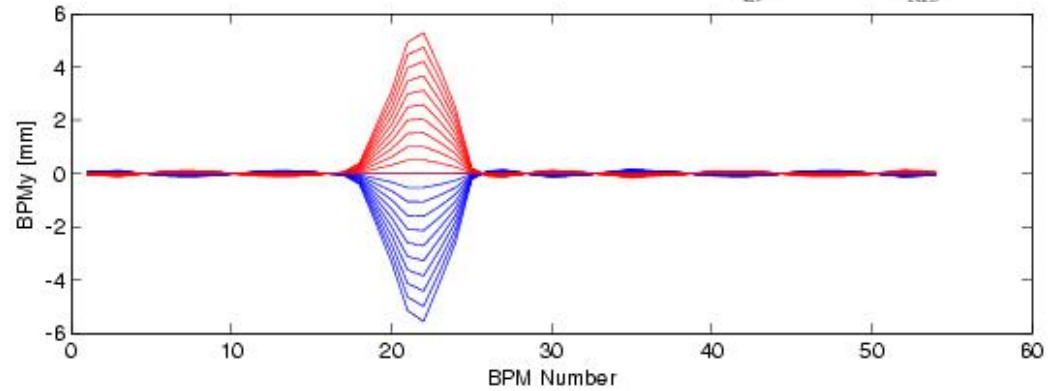
# Physical aperture probe

## Vertical beam bump in ID chamber

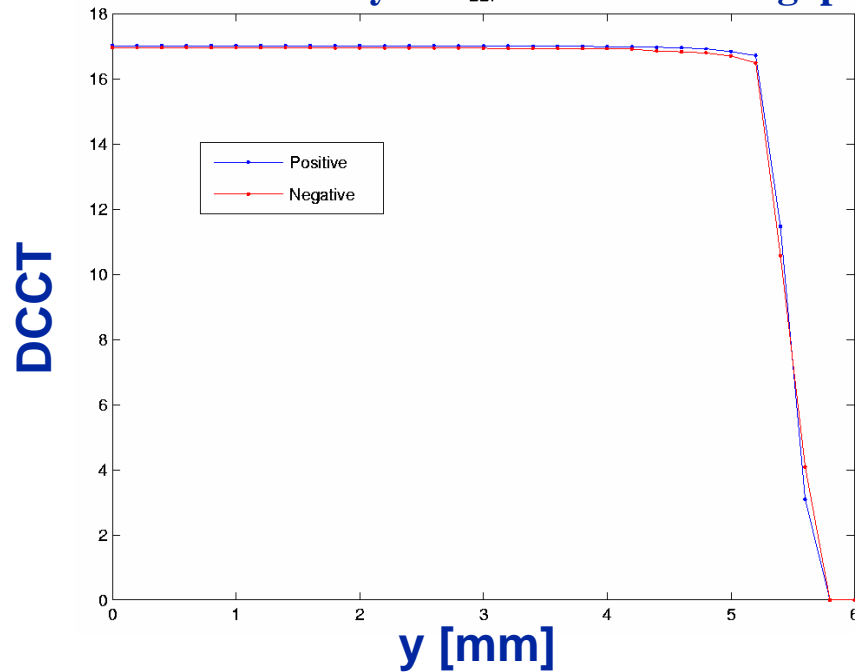


y-bump in ID chamber:

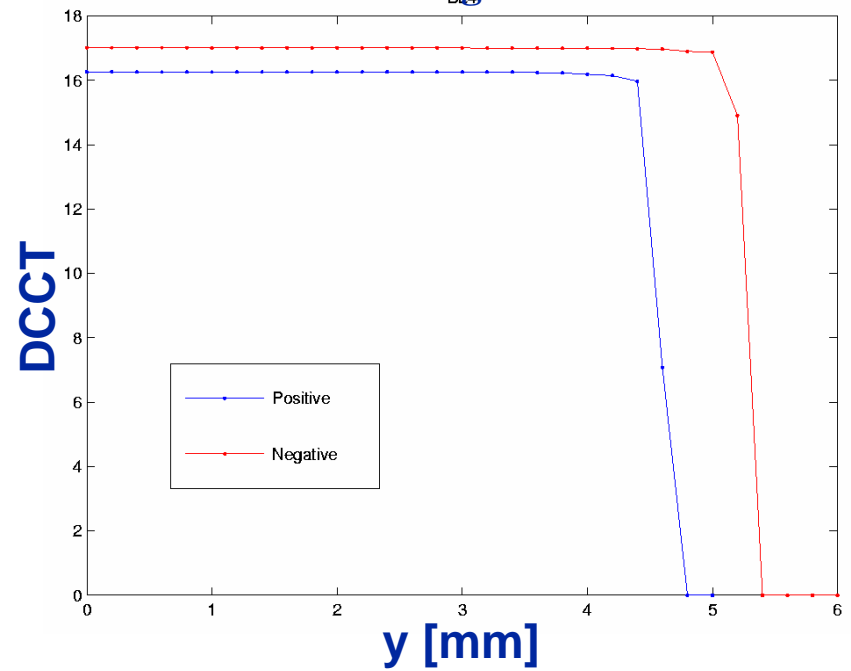
- Bump beam up until lost
- Refill
- Bump beam down until lost



ID7 chamber is symmetric and correct gap

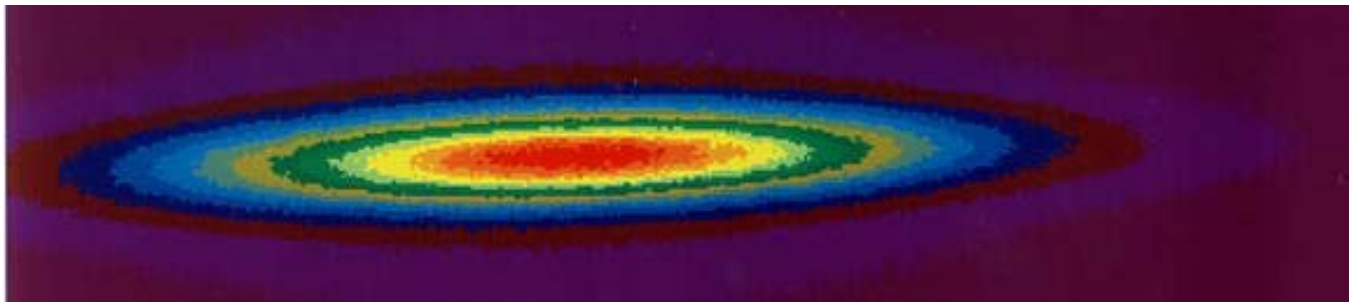
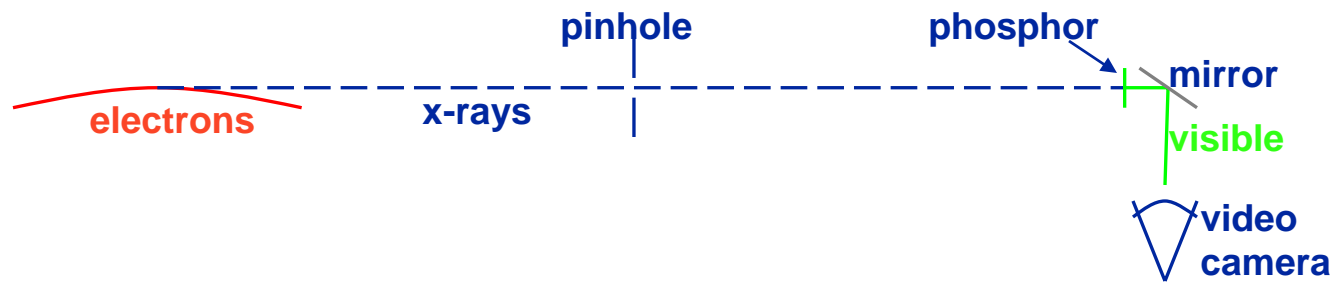


ID4 chamber is mis-aligned and too small



# Beam size measurements (more on Thurs.)

Synchrotron light monitors measure beam core



# Principle of streak camera

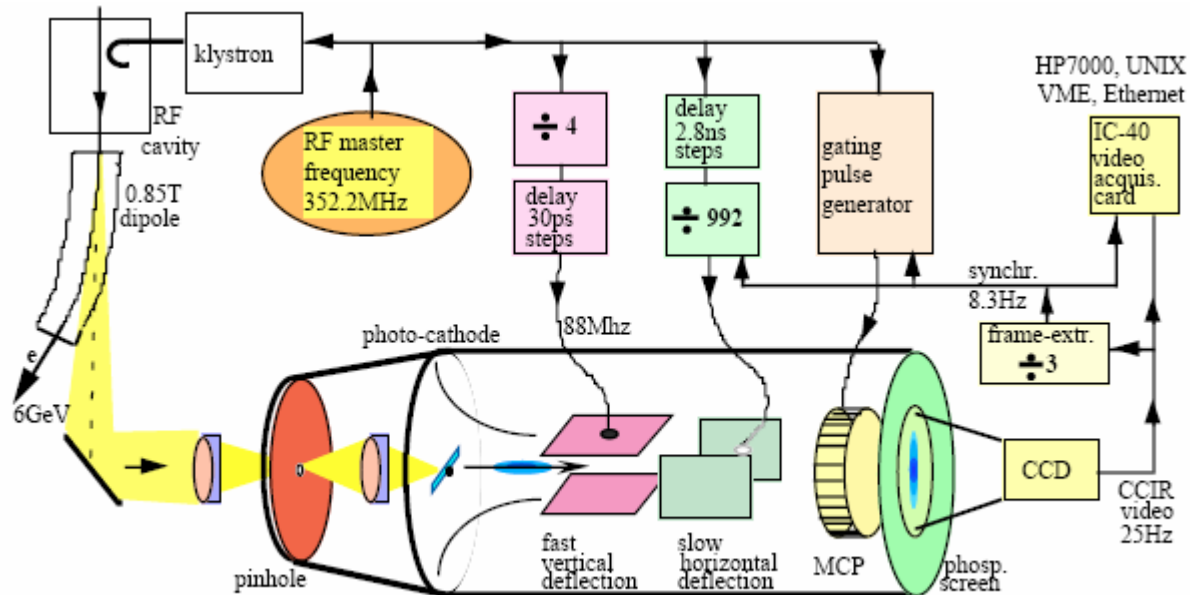
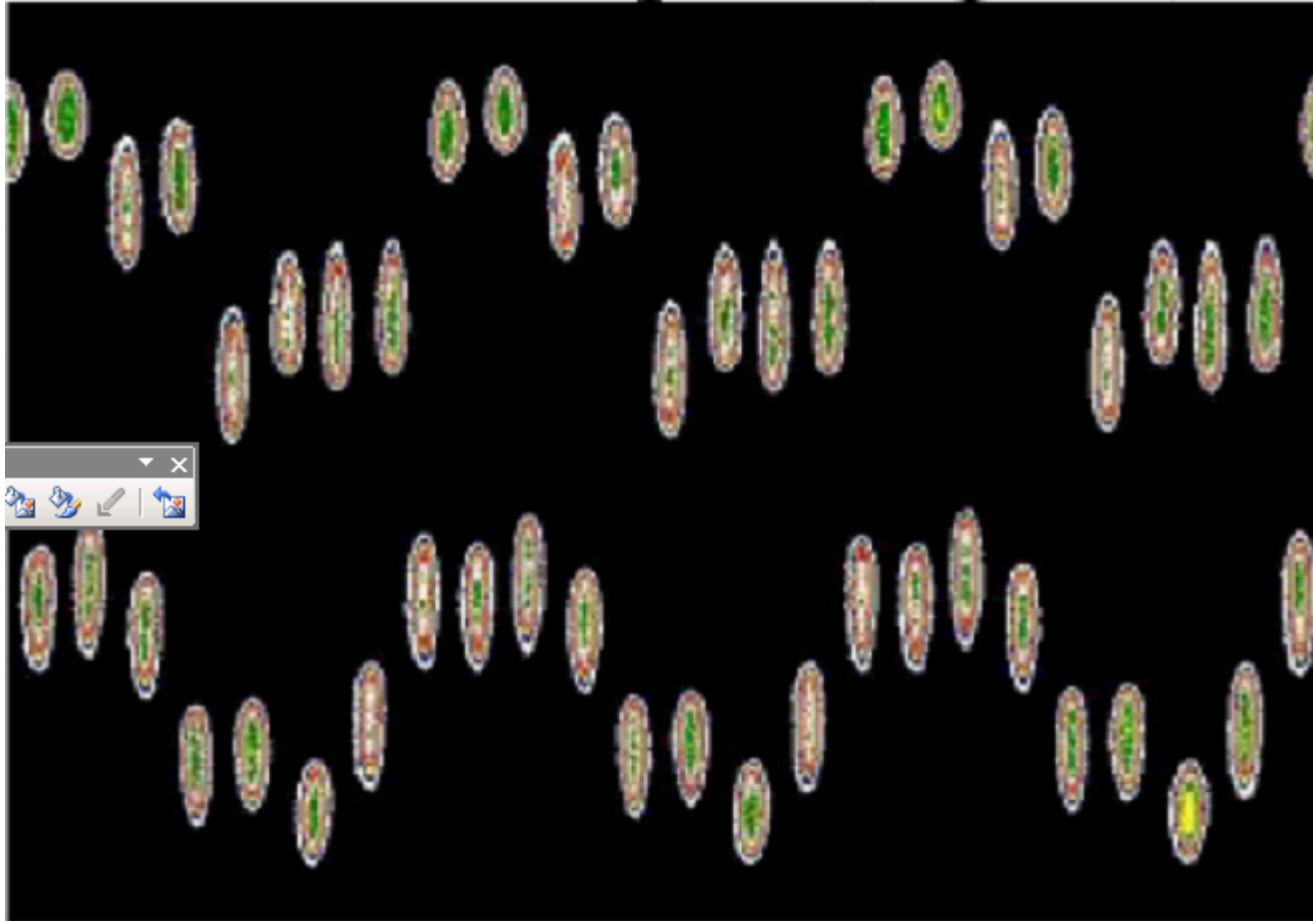
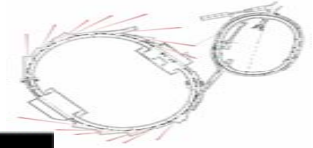


Figure: 1 Synchronisation of the Streak Camera system

- Convert light signal into electron beam (photo cathode)
- Accelerate electrons
- Use fast deflection to translate time delay into position difference
- In many ways similar to CRT ...

# Streak camera

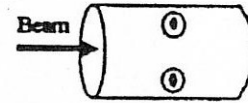
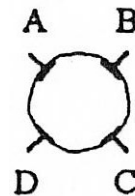


**Longitudinal instabilities at ESRF**

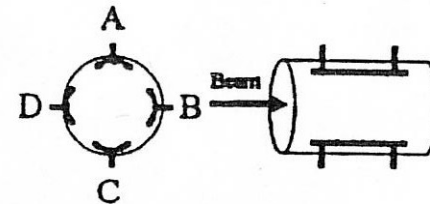
# Beam position monitors



$$x = \frac{r}{\sqrt{2}} \frac{(V_A + V_D - V_B - V_C)}{(V_A + V_B + V_C + V_D)}$$



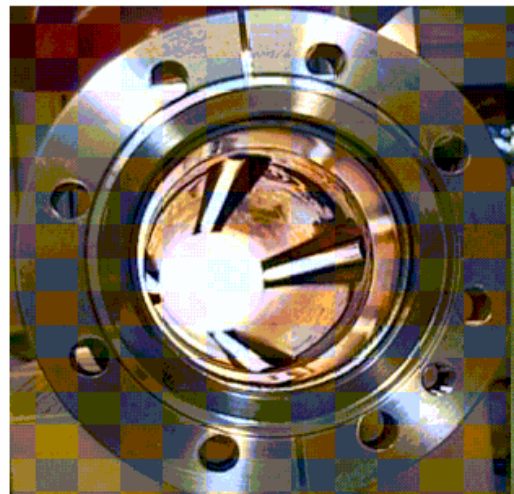
Buttons



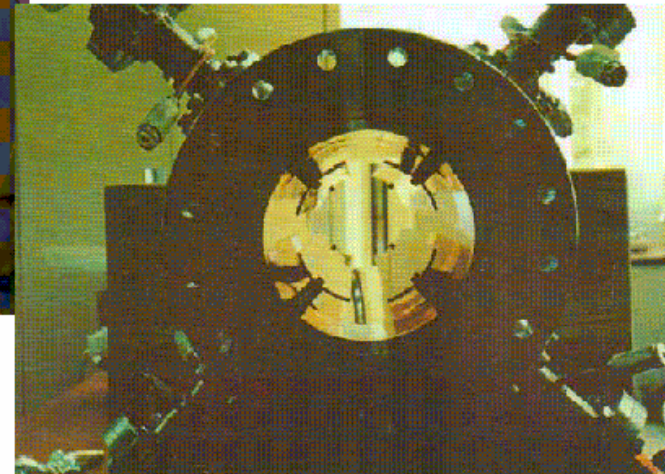
Striplines

**Electron BPM buttons sample electric fields; striplines couple to electric and magnetic fields.**

## Striplines



M. Wendt, DESY



M. Tobiyama, KEK

# Capacitive Pickups, Button BPMs



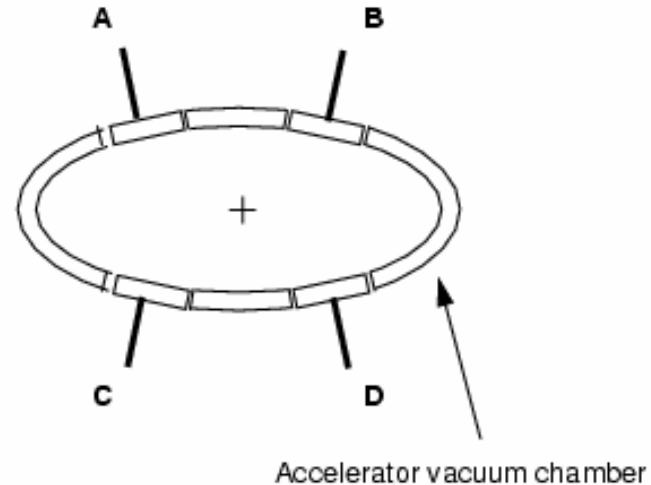
## Charged Particle Beam Pickup Electrodes

### Capacitive buttons

- Broadband, up to > 10 GHz
- Most effective when button diameter is comparable to the bunch length
- Minimal wakefield interaction with beam

$$X = K_x \frac{A-B+C-D}{A+B+C+D}$$

$$Y = K_y \frac{A+B-C-D}{A+B+C+D}$$



e.g. for round buttons of radius  $a$  in round pipe of radius  $r$

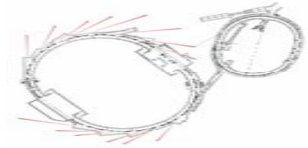
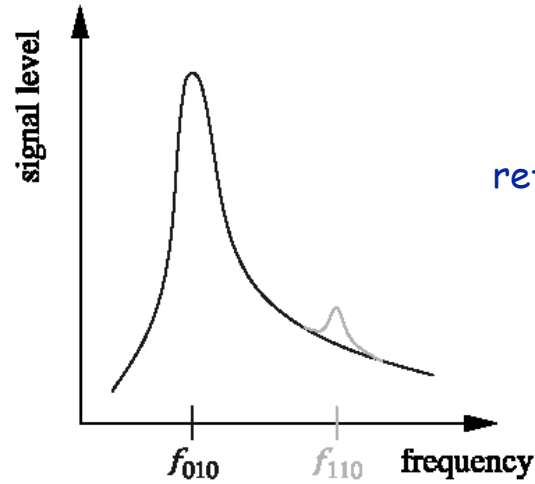
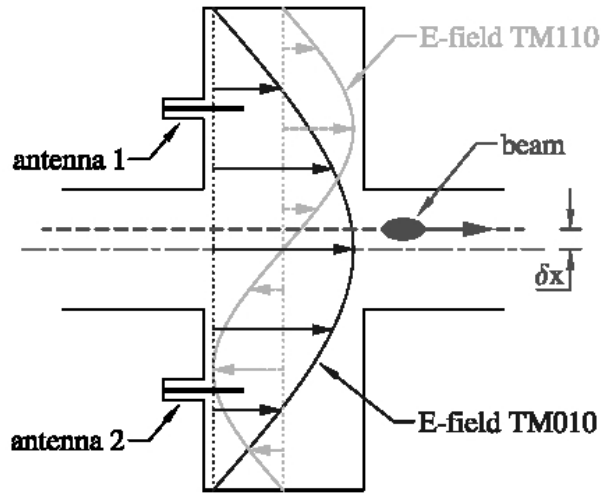
$$Z_t(\omega) = V_p / I_b = \frac{a^2 \omega}{2 r \beta c} \frac{R}{(1 + j\omega RC)}$$

where  $\beta = v/c$ ,

$R$  = Transmission line impedance,

$C$  = Button capacitance

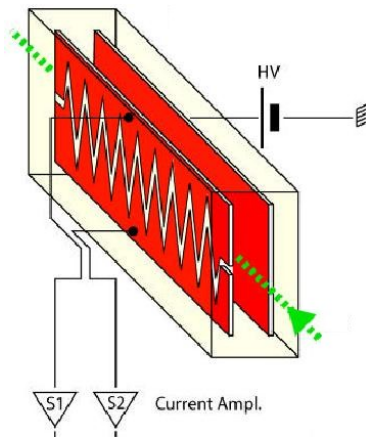
# CAVITY BPMs:



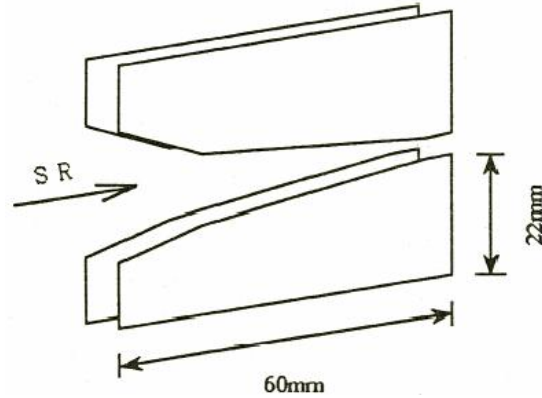
reference:  
 "Cavity BPMs", R. Lorentz  
 (BIW, Stanford, 1998)

# PHOTON BPMs:

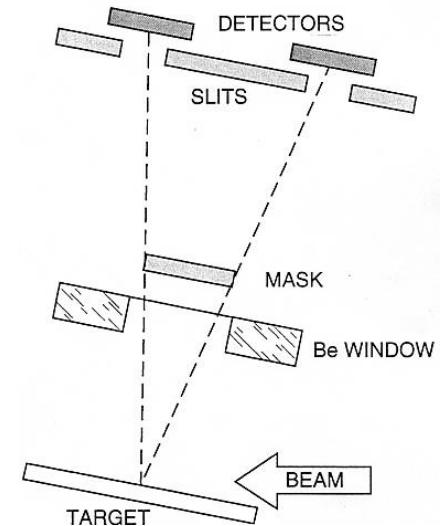
Split ion chamber:



Tungsten blade monitor:

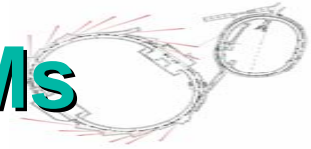


Copper fluorescence bpm:



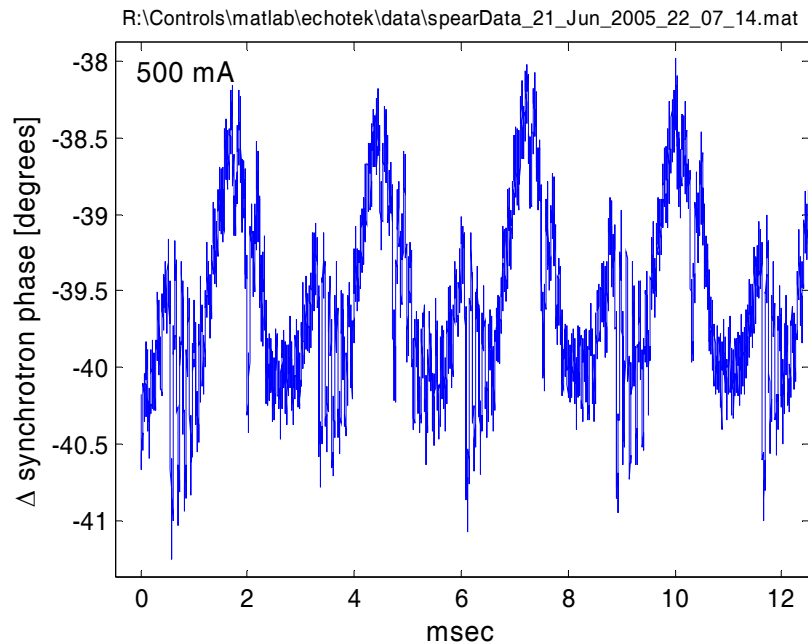


# Longitudinal oscillations, BPMs

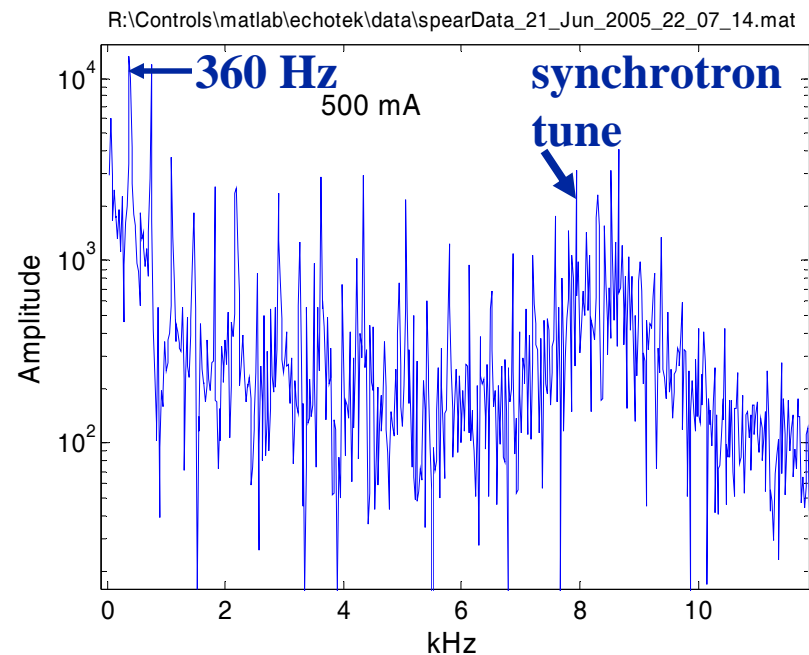


SPEAR3 digital receiver BPMs measure not only the amplitude from each button, but also the phase with respect to the RF, giving the variation in time of arrival of the bunches.

## Synchrotron phase vs. time



## FFT of synchrotron motion



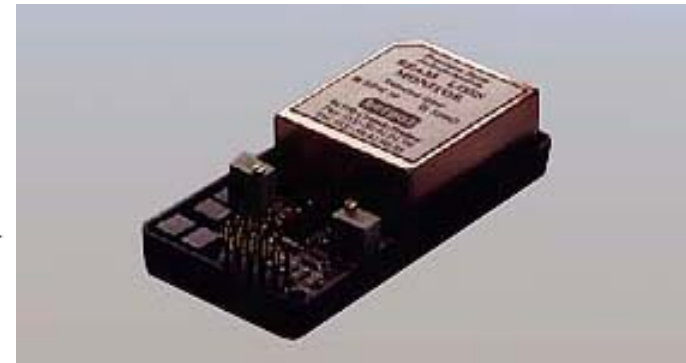
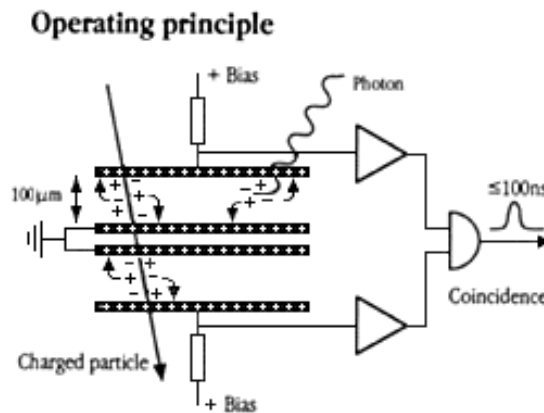
# Beam loss monitors



Electrons hit vacuum chamber and generate e<sup>+</sup>/e<sup>-</sup> shower which can be detected with beam loss monitors. Advantages over DCCT:

- Large dynamic range – can measure small losses
- Can localize losses for injected and stored beam
  - Losses at small vertical gaps (insertion devices) from Coulomb scattering.
  - Losses at high dispersion locations (Touschek scattering).

Bergoz PIN diodes generate pulses when from ionizing particles.

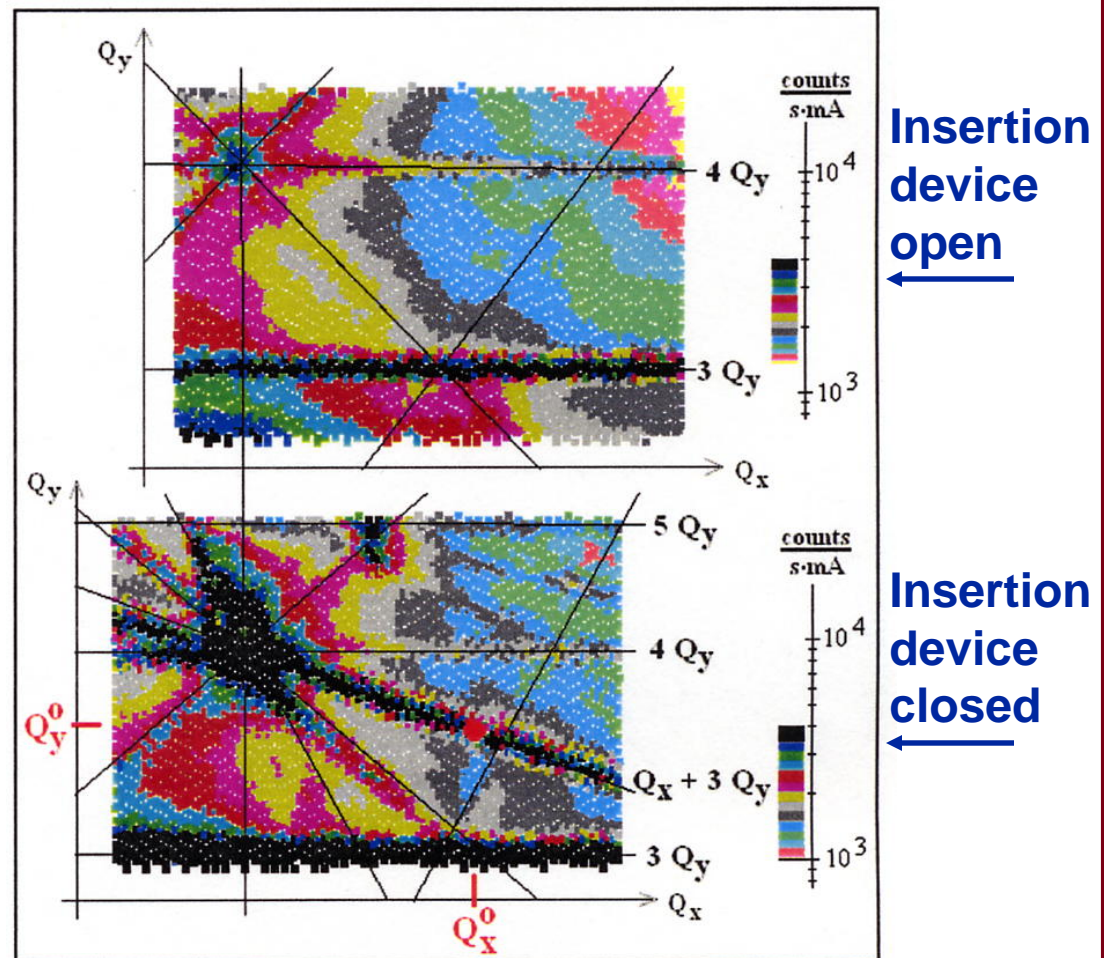


A scintillator with a photomultiplier is another commonly used BLM.

# Beam loss monitor measurement

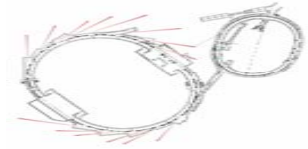


At BESSY, the beam loss was measured as a function of tunes. The additional losses associated with an insertion device showed a problem with nonlinear fields. (More on Thursday).



Kuske et al., PAC01.

# Beam frequencies

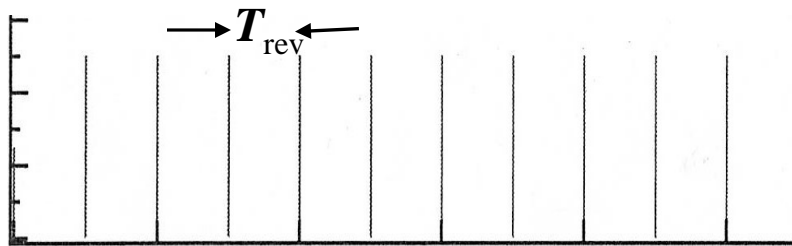


Using a spectrum analyzer with a BPM can yield a wealth of information on beam optics and stability. A single bunch with charge  $q$  in a storage ring with a revolution time  $T_{\text{rev}}$  gives the following signal on an oscilloscope

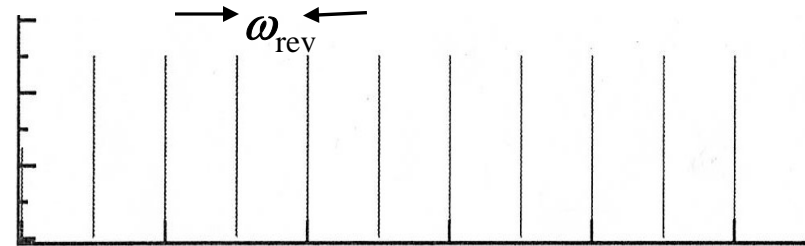
$$I(t) = \sum_{n=-\infty}^{\infty} q\delta(t - nT_{\text{rev}}),$$

where I'm assuming a zero-length bunch. A spectrum analyzer would see the Fourier transform of this,

$$I(\omega) = \sum_{n=-\infty}^{\infty} q\omega_{\text{rev}}\delta(\omega - n\omega_{\text{rev}})$$



Time



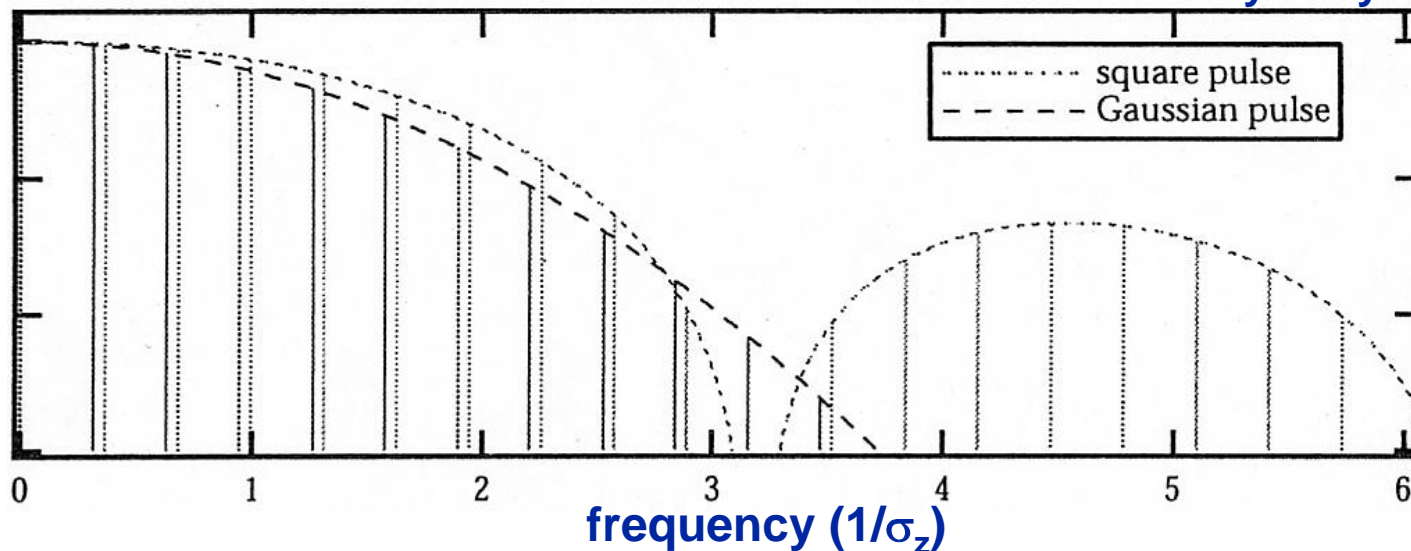
Frequency

# Spectrum for finite bunch length



For finite bunch length, the single bunch spectrum rolls off as the Fourier transform of the longitudinal bunch profile (Gaussian for e-rings).

Courtesy J. Byrd



For SPEAR3  $\sigma_z = 4.5$  mm, so  $c/\sigma_z = 67$  GHz.

# Betatron tune

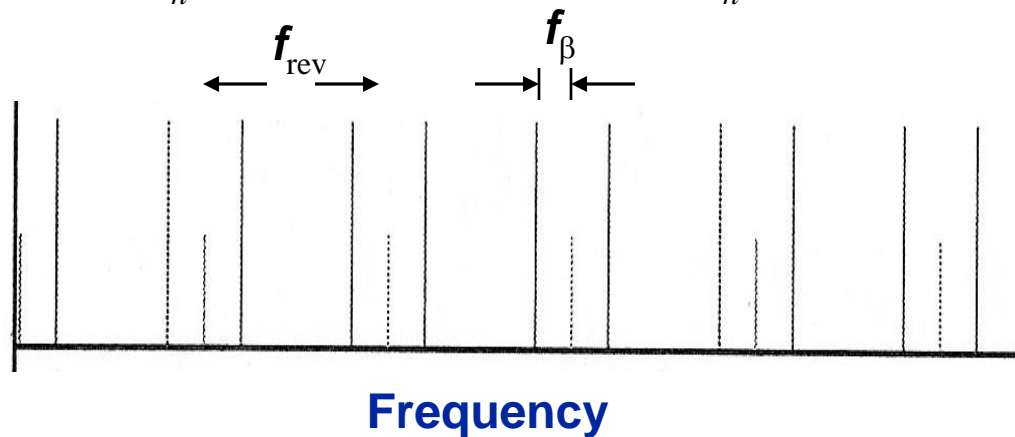


Combining BPM signals,  $V_A - V_B - V_C + V_D$ , gives a dipole signal that scales as the product of beam current and position. For a closed orbit  $x_{c.o.}$  and a betatron oscillation  $x_\beta$ , the signal is

$$d(t) = (x_{c.o.} + x_\beta \cos(2\pi\nu t)) \sum_{n=-\infty}^{\infty} q \delta(t - nT_{\text{rev}})$$

The Fourier transform is

$$d(\omega) = q\omega_{\text{rev}} x_{c.o.} \sum_n \delta(\omega - n\omega_{\text{rev}}) + q\omega_{\text{rev}} x_\beta \sum_n \delta(\omega - (\omega_\beta + n\omega_{\text{rev}}))$$

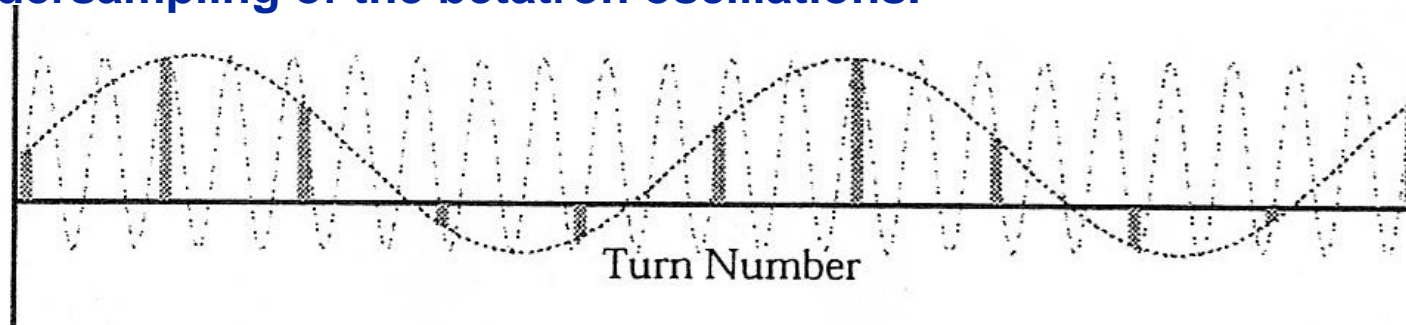


The tune is given by  $\nu = f_\beta / f_{\text{rev}}$  (with integer/half-integer ambiguity).

# Betatron tune, 2

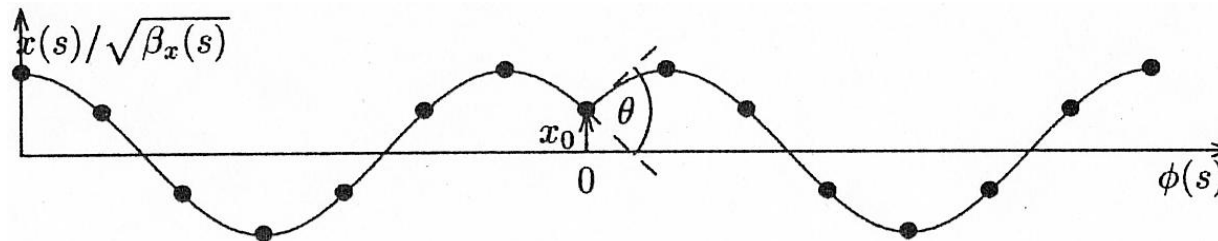


The integer/half-integer ambiguity in tune measurement arises from undersampling of the betatron oscillations.

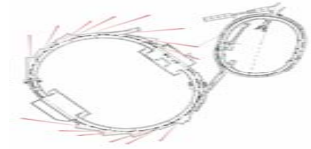


It can be resolved by measuring the shift in closed orbit from a single steering magnet.

$$\frac{\Delta x_i}{\Delta \theta_j} = \frac{\sqrt{\beta_i \beta_j}}{2 \sin(\pi \nu)} \cos(|\phi_i - \phi_j| - \pi \nu)$$

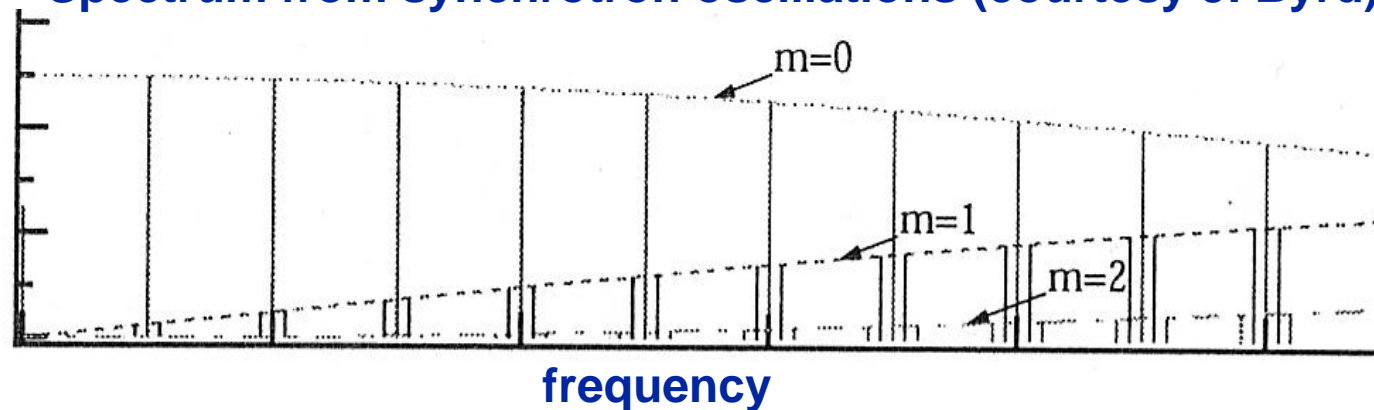


# Synchrotron tune



Synchrotron oscillations cause modulation of the arrival time of the beam by the synchrotron tune. This also shows up as sidebands around the revolution harmonics.

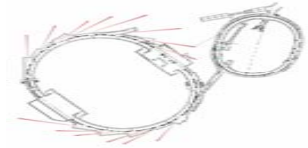
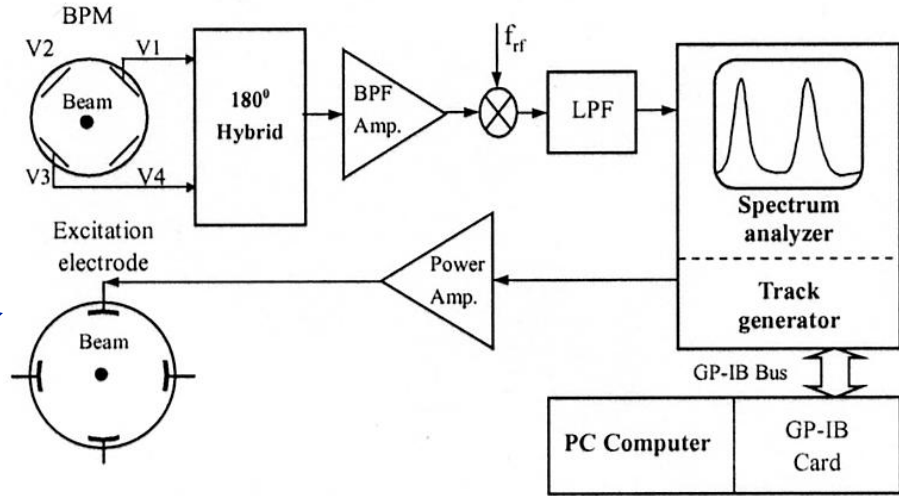
Spectrum from synchrotron oscillations (courtesy J. Byrd)





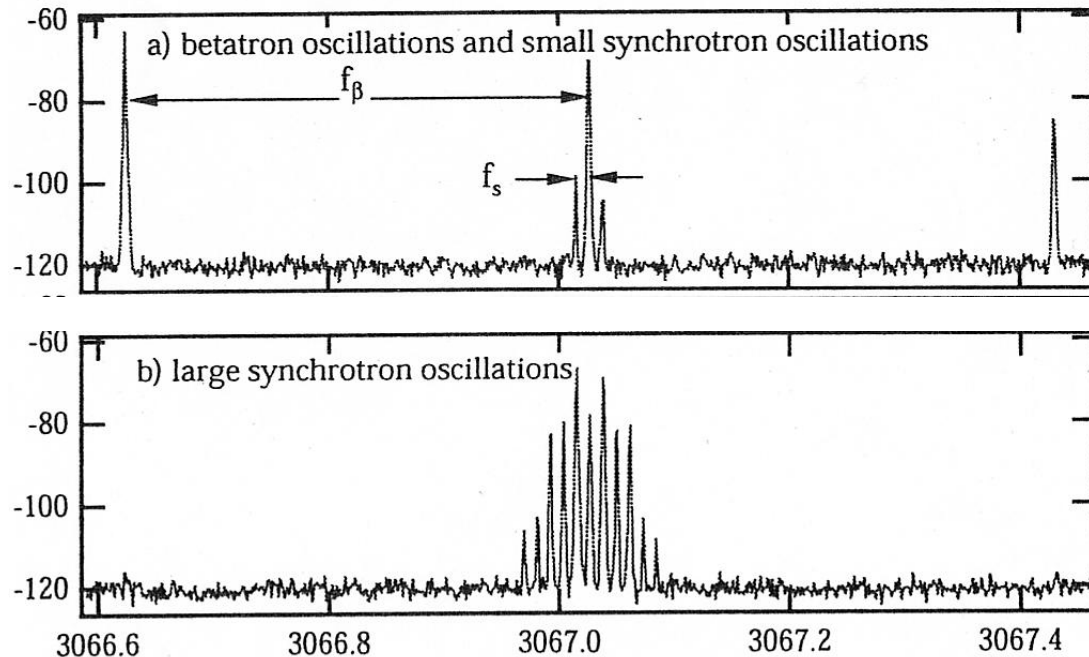
# Measured spectra

Typical tune measurement



HLS tune meas.,  
Sun et al. PAC01

Typical measured spectra



Multibunch spectra, instabilities, Steier, Friday.

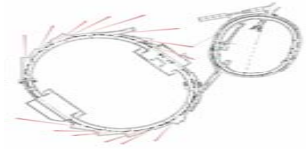
# More on spectrum



Tune measurements play an important role in many storage ring measurements.

- Turn by turn measurements, FFT, NAFF
- Betatron phase measurement (Tuesday)
- Nonlinear dynamics (tune vs. amplitude; tune vs. closed orbit; Thursday)
- Impedance measurements (Friday)
- Beta function measurements
- Chromaticity

# Beta function measurement



Beta functions can be measured by measuring the change in tune with quadrupole strength:

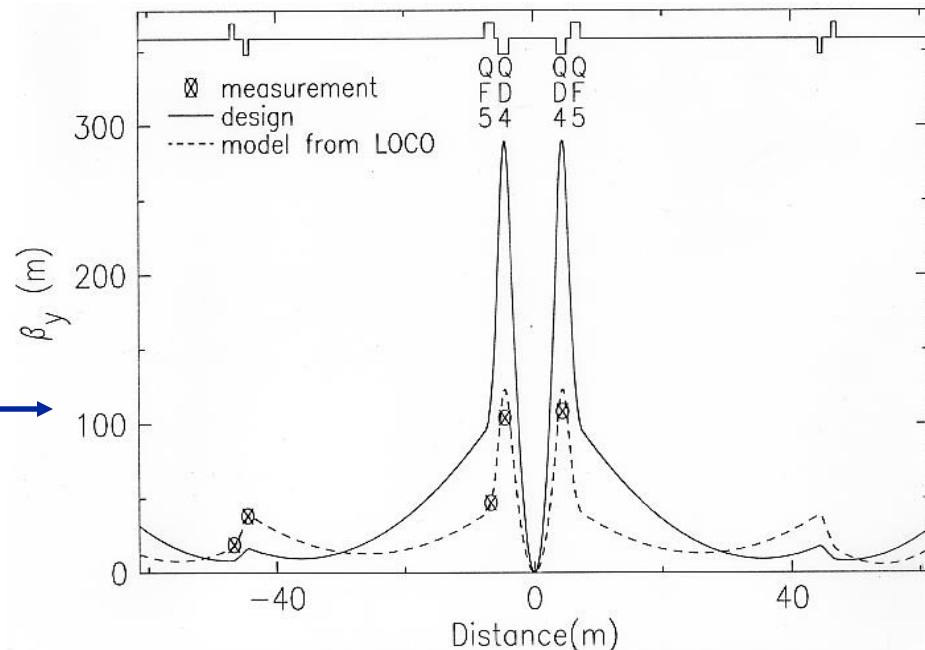
$$\Delta \nu = \beta \frac{\Delta(KL)}{4\pi}$$

## Measurement issues

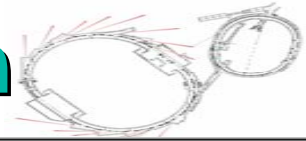
- Keep orbit constant
- Hysteresis
- Saturation
- Sometimes cannot vary individual quadrupoles

$\beta$  measurement in PEP-II HER IR indicates optics problem.

(Methods to be described Tuesday were used to find source of problem and correct it.)

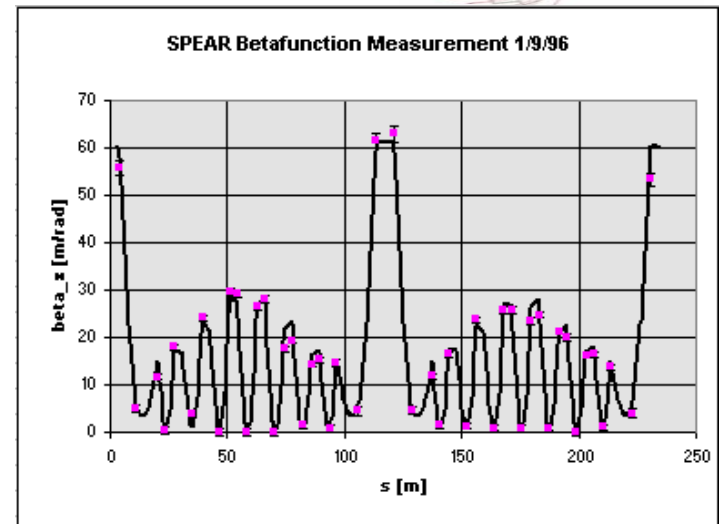


# SPEAR $\beta$ -function correction

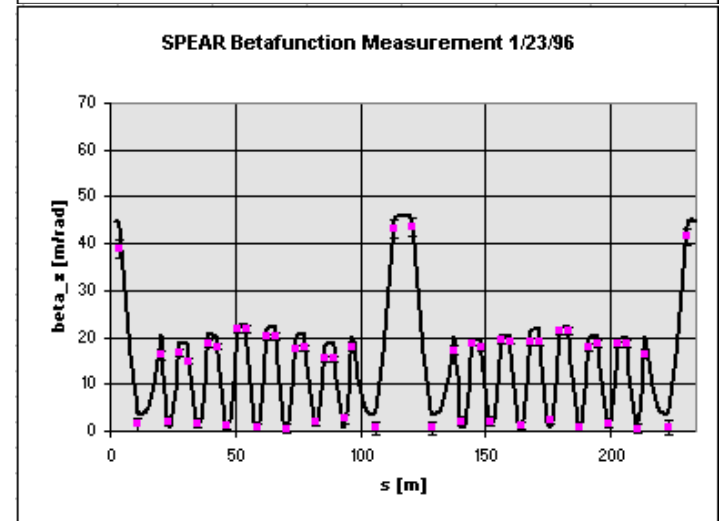


1.  $\beta$  functions measured at quads.
2. MAD model fit to measurements.
3. MAD quadrupoles adjusted to fix  $\beta$ 's.
4. Quadrupole changes applied to ring.
5.  $\beta$  functions re-measured at quads.
6. Iterate.

before



after



Courtesy Heinz-Dieter Nuhn

# Other $\beta$ measurements



1. Fit  $\beta$  and  $\phi$  to measured orbit response matrix (Y. Chung et al., PAC'93)

$$M_{ij} = \frac{\Delta x_i}{\Delta \theta_j} = \frac{\sqrt{\beta_i \beta_j}}{2 \sin(\pi \nu)} \cos(|\phi_i - \phi_j| - \pi \nu)$$

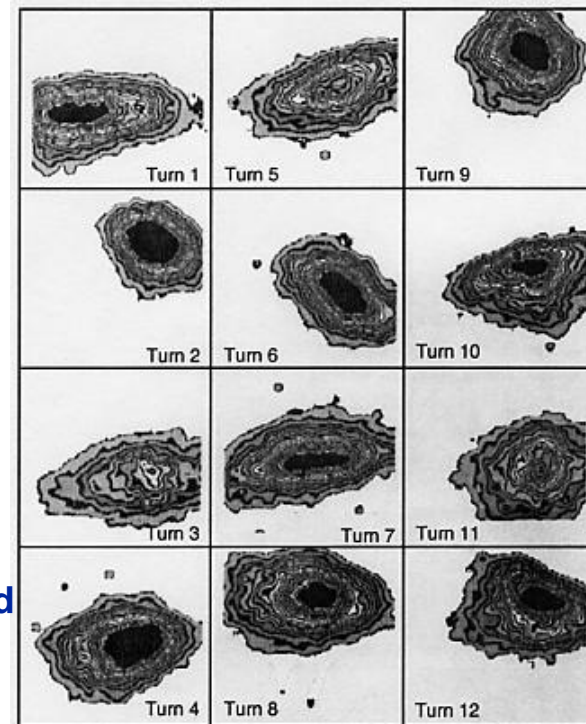
$N_{\text{BPM}} * N_{\text{steerer}}$  data

$2 * N_{\text{BPM}} + 2 * N_{\text{steerer}} + 1$  unknowns

2. Fit quadrupole gradients, K, to measured orbit response matrix. From K get  $\beta$  (Tuesday lecture).
3. Derive from betatron phase measurements (Tuesday lecture).
4. Beam size measurement

$$\sigma = \sqrt{\epsilon \beta}$$

Measuring  $\beta$  mismatch; injected beam; SLC damping rings.



Minty and Spence, PAC'95

# Dispersion



Dispersion is the change in closed orbit with a change in electron energy.

$$\eta \equiv \Delta x / \frac{\Delta p}{p}$$

The energy can be changed by shifting the rf frequency.

$$\alpha \equiv \frac{\Delta L}{L} / \frac{\Delta p}{p} \quad \Rightarrow \quad \frac{\Delta p}{p} = -\frac{1}{\alpha} \frac{\Delta f_{rf}}{f_{rf}} \quad (\alpha = \text{momentum compaction})$$

So the dispersion can be measured by measuring the change in closed orbit with rf frequency.

$$\eta = -\alpha f_{rf} \frac{\Delta x}{\Delta f_{rf}}$$

# Dispersion measurement

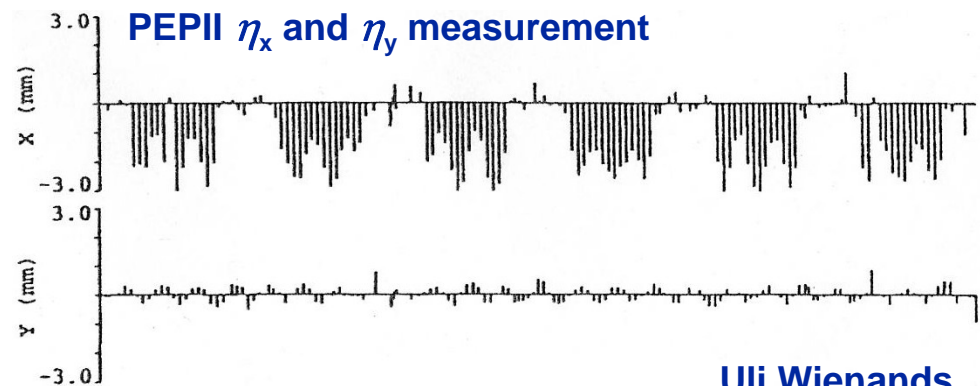
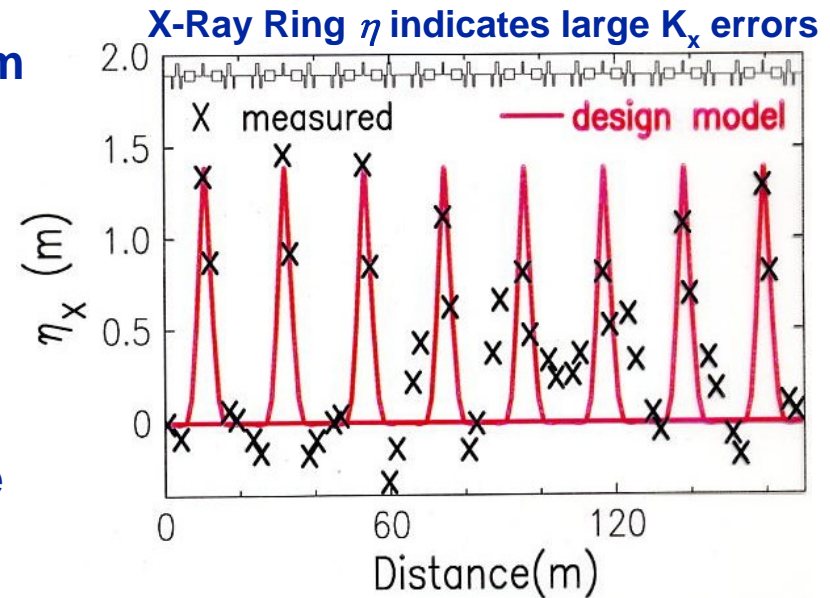


Dispersion distortion can come from quadrupole or dipole errors.

$$\eta_x'' + K_x \eta_x = \frac{1}{\rho_x}$$

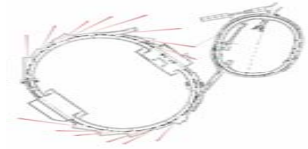
Vertical dispersion gives a measure of vertical bending errors or skew gradient errors in a storage ring.

$$\eta_y'' + K_y \eta_y = \frac{1}{\rho_y} + K^{\text{skew}} \eta_x$$



Uli Wienands

# Chromaticity



Quadrupoles focus high energy particles less than low energy particles. This leads to a decrease in tune with energy (natural chromaticity):

$$\xi_N = \Delta \nu / \frac{\Delta p}{p}$$

Decrease in tune with energy is corrected with sextupoles (position dependent focusing),

$$K = mx = m\eta \Delta p / p$$

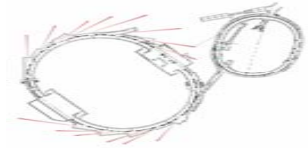
$K$  is the gradient,  $m$  is the sextupole strength.

The chromaticity with sextupoles is called the corrected chromaticity,

$$\xi$$



# Chromaticity measurement



To measure the chromaticity, the beam energy can be changed in one of two ways:

1. Change the rf frequency. This shifts the orbit in sextupoles, giving the corrected chromaticity.

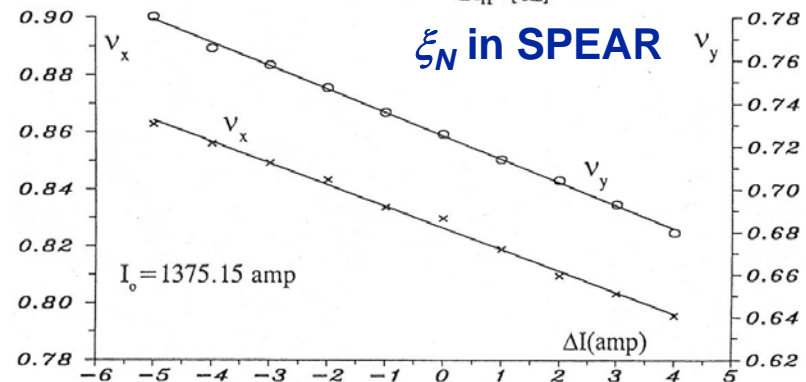
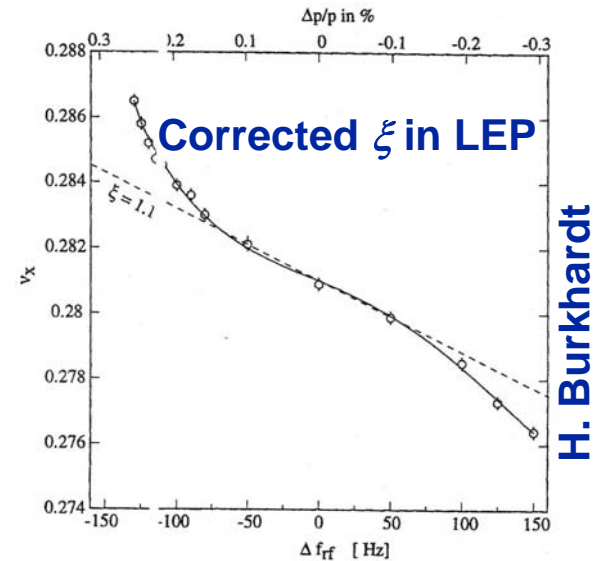
$$\xi = -\alpha f_{rf} \frac{\Delta v}{\Delta f_{rf}}$$

Used to diagnose sextupole miswiring in PEP-II-HER.

2. Change the dipole field. This keeps orbit constant, measuring the natural chromaticity.

$$\xi_N = \frac{\Delta v}{\Delta B/B}$$

$\xi_N$  can also be measured from  $n$  vs.  $frf$  with sextupoles turned off.



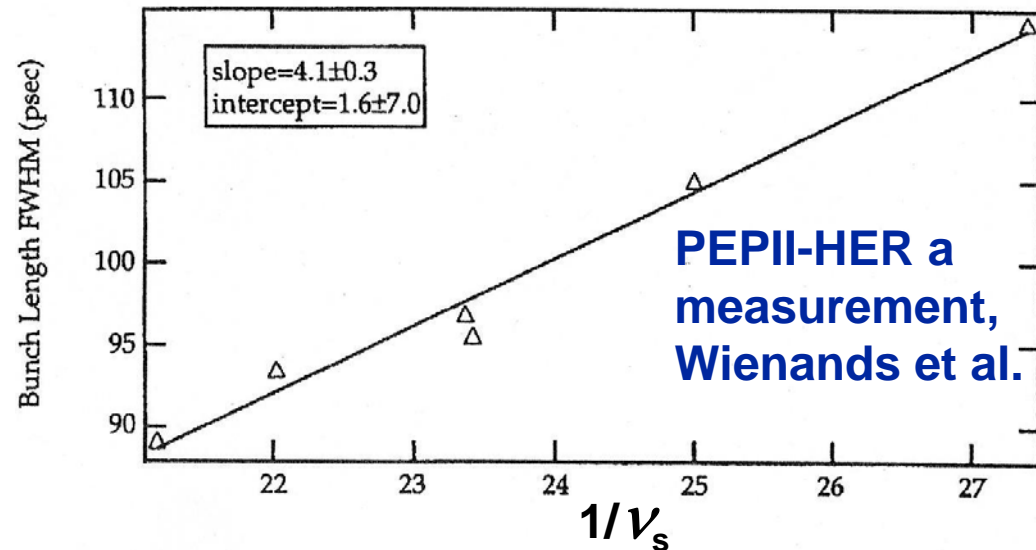
# Momentum compaction



Using the model value of  $\alpha$  for  $\xi$  and  $\eta$  measurements can lead to errors.  
 $\alpha$  itself can be measured in various ways.

Indirect measurement from bunch length

$$\sigma_z = \frac{c \sigma_\delta}{2\pi f_{\text{rev}}} \frac{\alpha}{v_s}$$

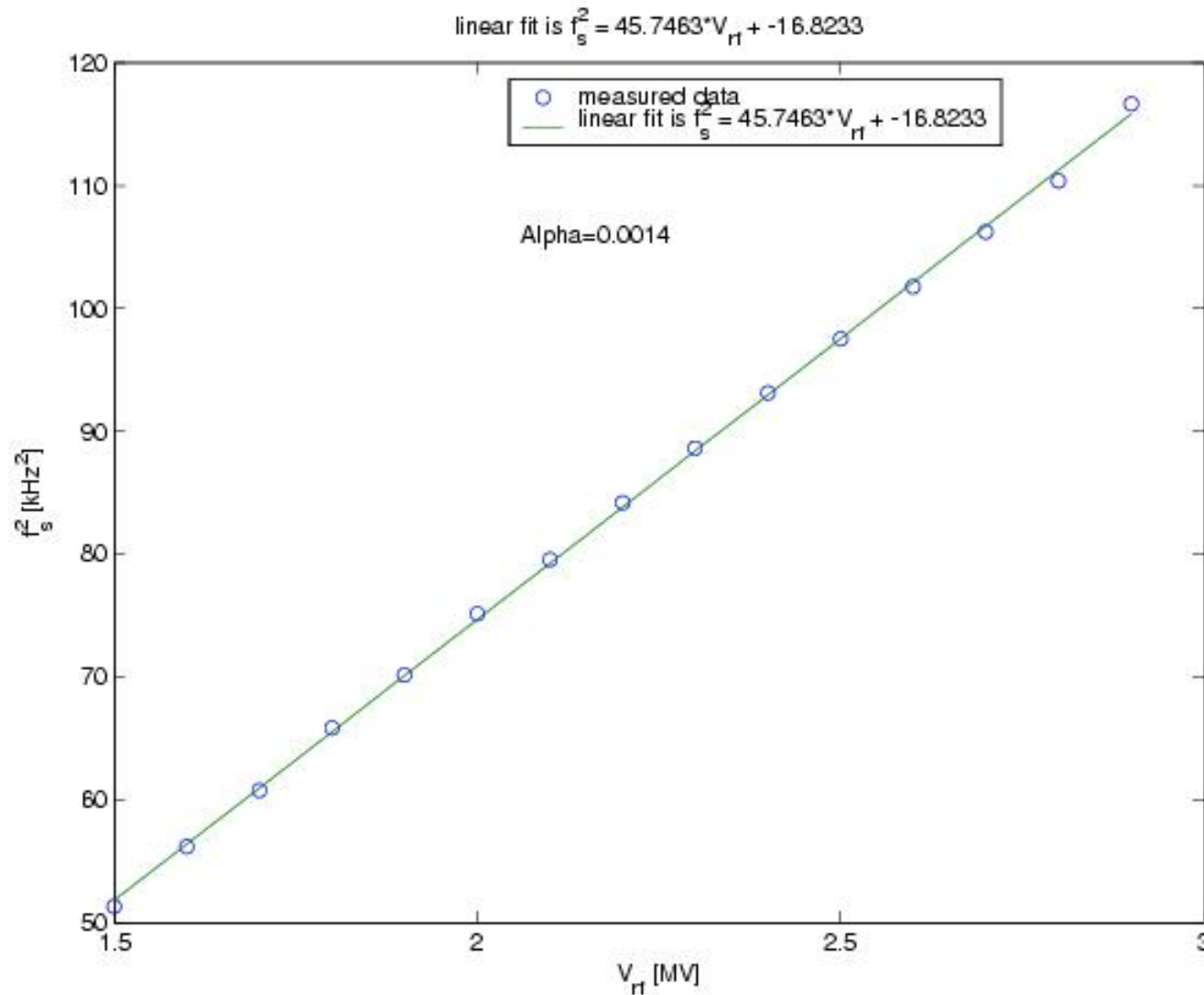


Direct measurement: measure change in energy with rf frequency.

$$\alpha = - \frac{\Delta f_{\text{rf}} / f_{\text{rf}}}{\Delta p / p}$$

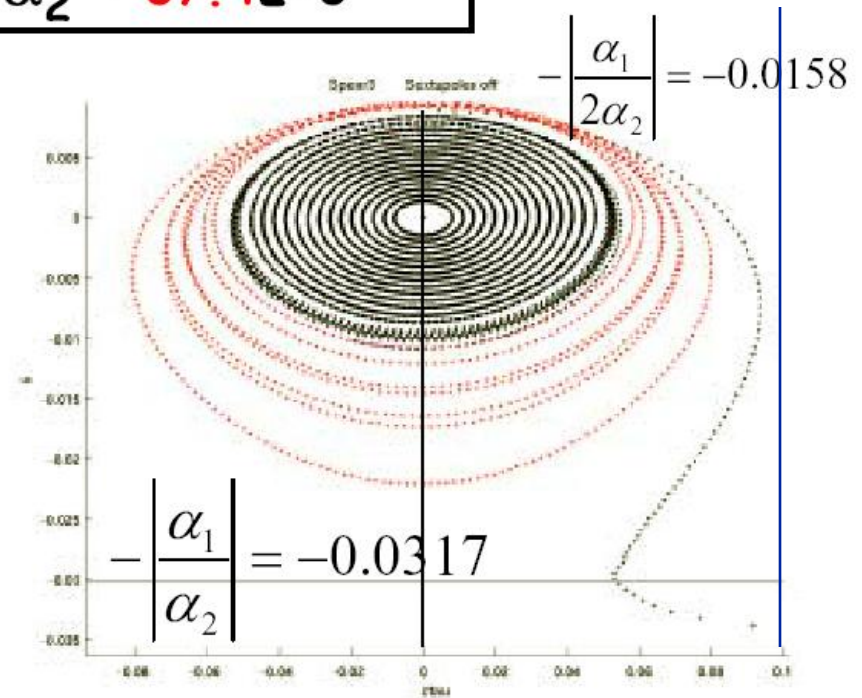
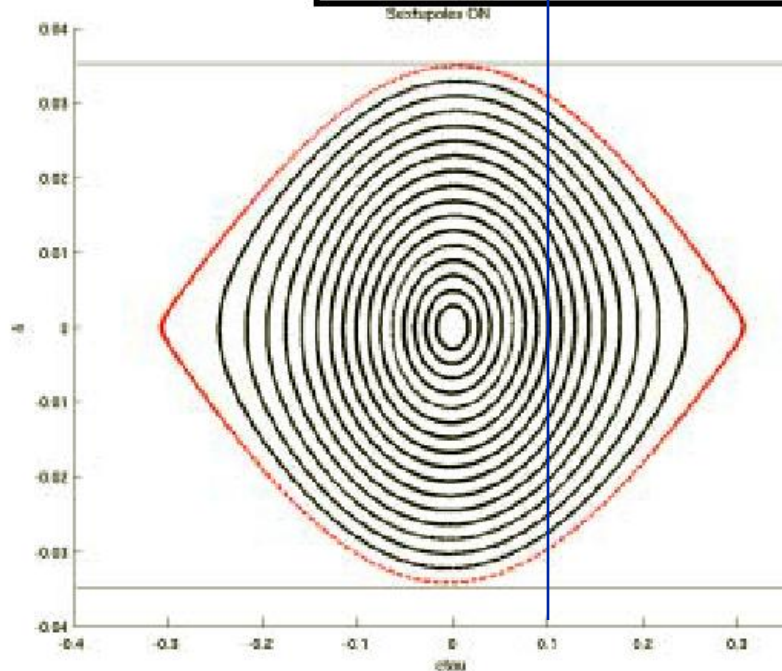
Friday will include lecture on energy measurement.

# Momentum compaction measurement



# SPEAR3: Longitudinal Dynamics

Sextupoles on	Sextupoles off
$\alpha_1 = 1.19 \text{ E-3}$	
$\alpha_2 = -2.1\text{E-3}$	$\alpha_2 = 37.4\text{E-3}$

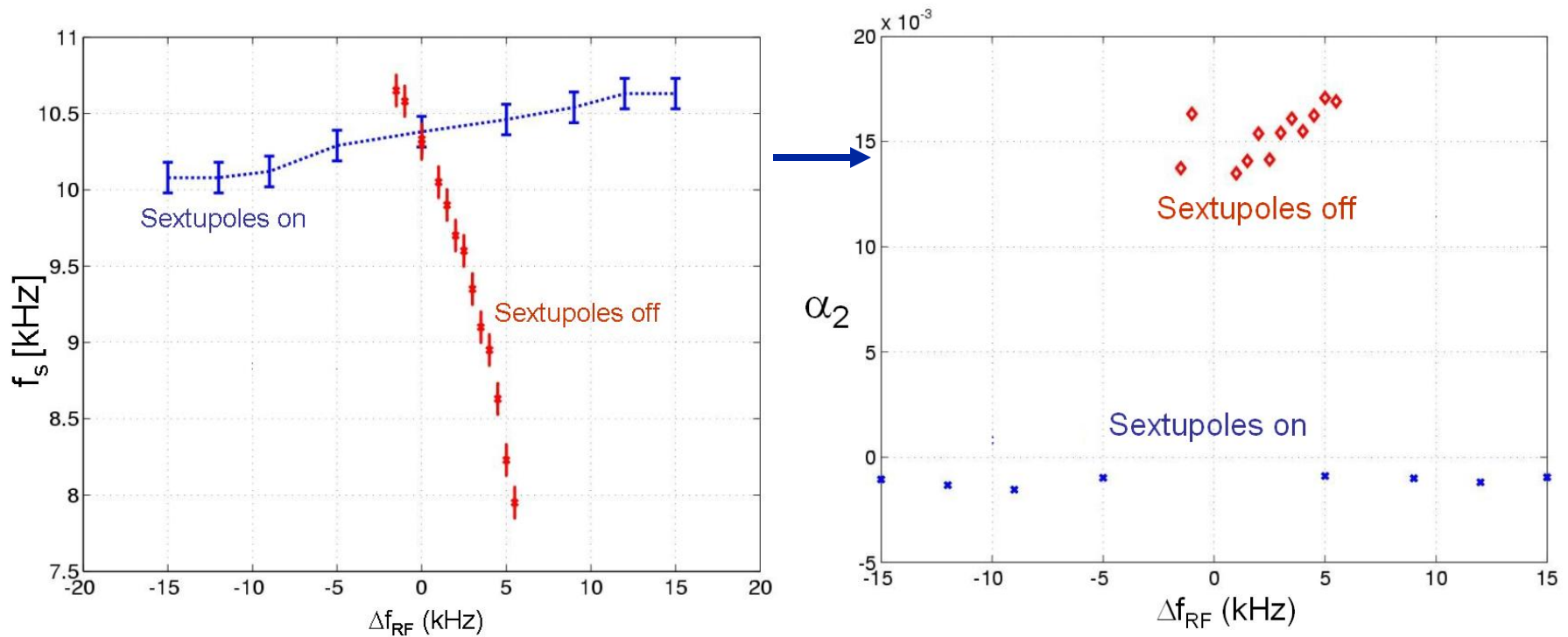


4D tracking using AT

# $\alpha_2$ measurement



- $|\alpha_2|$ , sextupoles off  $\gg$   $|\alpha_2|$ , sextupoles on
- Energy aperture much reduced with sextupoles off



# Further reading



For more on beam measurements, see:

Beam Measurement, Proceedings of the Joint US-CERN-Japan-Russia School on Particle Accelerators, S-I. Kurokawa, S.Y. Lee, E. Perevedentsev & S. Turner, editors, World Scientific (1999).

My lecture was in particular derived from lectures in Beam Measurement by Frank Zimmermann and John Byrd. The lectures by Frank Zimmermann are given in more detail in a new book:

M.G. Minty and F. Zimmermann, Measurement and control of charged particle beams, Springer (2003).