



How (transverse) single particle dynamics determines injection efficiency, lifetime, ...

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- Outline:
 - Motivation
 - •Lifetime limiting processes
 - •Tunescans
 - •Frequency Maps
 - •On energy dynamic aperture: Injection Efficiency
 - •Momentum aperture: Touschek Lifetime

Concepts



Want to touch on a number of measurement methods including:

- Scraper measurements
- RF scans
- Tune scans
- Pinger measurements
- Frequency Map Analysis

Motivation



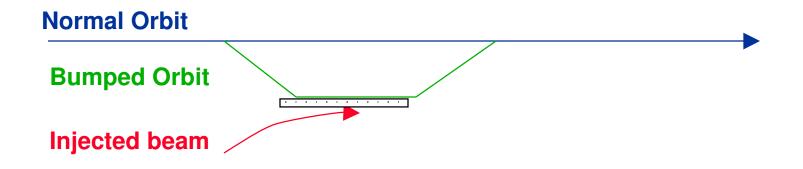
Motion of particles at large amplitudes impacts the performance of the storage ring.

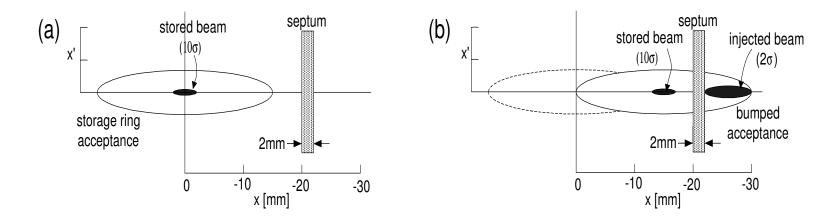
Particle loss

- Injection efficiency
 - Longer injection times
 - Increased radiation levels
- Lifetime
 - More frequency fills
 - Faster current loss → changing brightness

Injection Efficiency







Storage ring acceptance has to be large enough to capture sufficient amount of injected beam – Often limited by dynamic aperture.

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Lifetime and beam loss



Why is there a finite lifetime?

- Electron undergoes a scattering event
- Change in angle or energy gives increased amplitude of oscillation
- If a boundary is hit (physical or dynamic) then the electron is lost
- Gradually all electrons are lost

Types of scattering



Types of scattering

- Electron-Photon Scattering
 - Quantum Lifetime
- Electron-Gas Scattering
 - Gas Lifetime
- Electron-Electron Scattering
 - Touschek Lifetime

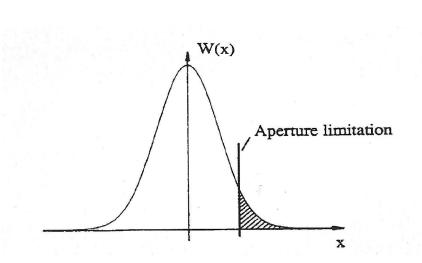
Quantum Lifetime

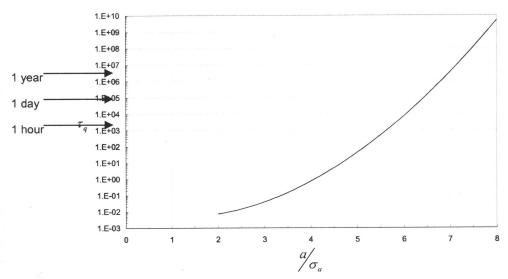


- Emission of synchrotron radiation is quantized
- Distribution of radiation is approximately Gaussian
- A Gaussian distribution of particles is produced
- Tails of distribution are lost
- Redistribution on time scale of damping time
- Quantum lifetime is typically more important for colliders than for light sources

Quantum Lifetime







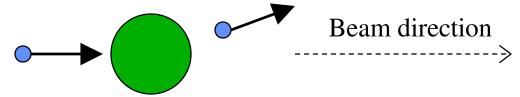
Beam distribution, W(x)

Quantum Lifetime versus aperture-to-beamsize ratio

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Gas-scattering lifetime

Particles scatter elastically or inelastic with residual gas atoms. This introduces betatron or synchrotron oscillations.



The scattering process can be described by the classical Rutherford scattering with differential cross section per atom in cgs units

$$\frac{d\sigma}{d\Omega} = \left(\frac{zZe^2}{2\beta cp}\right) \frac{1}{\sin^4 \frac{\theta}{2}}$$

If the new amplitudes are outside the aperture the particles are lost.

The elastic scattering lifetime is proportional to the square of the transverse aperture *A*:

$$\frac{1}{\tau_{el}} \propto \frac{1}{E^2} \times \left(\frac{\beta_x}{A_x^2} \langle P \beta_x \rangle + \frac{\beta_y}{A_y^2} \langle P \beta_y \rangle \right)$$

The inelastic scattering lifetime is proportional to the logarithm of the longitudinal aperture ϵ :

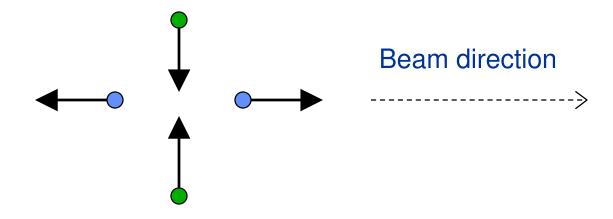
$$\frac{1}{\tau_{inel}} \propto \langle P \rangle \times \ln(\varepsilon)$$

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Touschek Lifetime



Particles inside a bunch perform transverse betatron oscillations around the closed orbit. If two particles scatter they can transform their transverse momenta into longitudinal momenta.



Touschek Scattering



- Large angle electron-electron scattering
 - → single scattering leads to loss
- Calculate scattering cross-section: Møller cross section, which reduces to $d\sigma < \frac{1}{\beta^2} \left(\frac{1}{\sin^4 \theta} \frac{1}{\sin^2 \theta} \right) d\Omega$
- Above formula is correct for non relativistic velocities (in restframe of particle bunch) and if there is no average polarization
 - In reality effect of polarization not negligible (see my talk on Friday)
- If the new momenta of the two particles are outside the momentum aperture, ε , the particles are lost. The lifetime is proportional to the square of ε

$$\frac{1}{\tau_{tou}} \propto \frac{1}{E^3} \frac{I_{bunch}}{V_{bunch} \sigma_x} \frac{1}{\varepsilon^2} f(\varepsilon, \sigma_x, E)$$

What determines the size of the momentum aperture, ε ?

Lifetime Limiting Processes



Elastic Scattering

$$\frac{1}{\tau_{el}} \propto \frac{1}{E^2} \times \left(\frac{\beta_x}{\Delta_x^2} \langle P\beta_x \rangle + \frac{\beta_y}{\Delta_y^2} \langle P\beta_y \rangle\right) \tag{1}$$

❖ Touschek Effect

$$\frac{1}{\tau_{tow}} \propto \frac{1}{E^3} \frac{I_{bunch}}{V_{bunch} \sigma_x} \frac{1}{\varepsilon} f(\varepsilon, \sigma_x, E)$$
 (2)

Quantum Lifetime

$$\frac{1}{\tau_a} \propto \frac{\Delta^2}{\sigma^2} \times \exp(-\frac{\Delta^2}{2\sigma^2})$$
 (3)

Inelastic Scattering

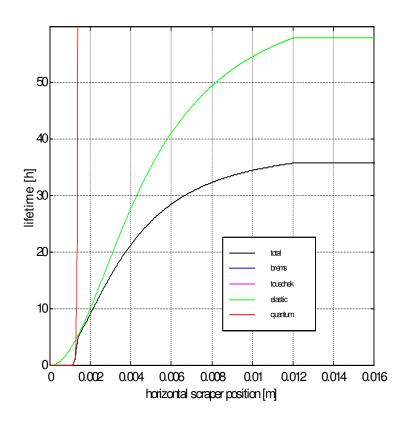
$$\frac{1}{\tau_{inel}} \propto \langle P \rangle \times \ln(\varepsilon) \tag{4}$$

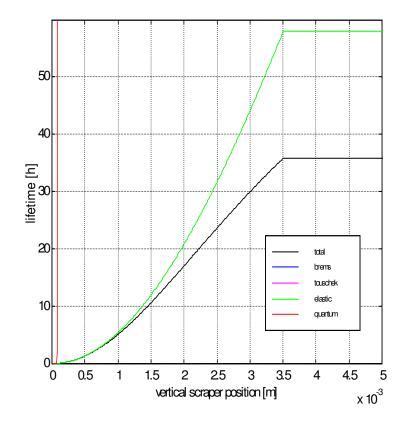
$$\frac{1}{\tau} = \frac{1}{\tau_{el}} + \frac{1}{\tau_{tou}} + \frac{1}{\tau_{gl}} + \frac{1}{\tau_{inell}}$$

Dependency of Lifetime on Transverse Aperture



Theoretical Results

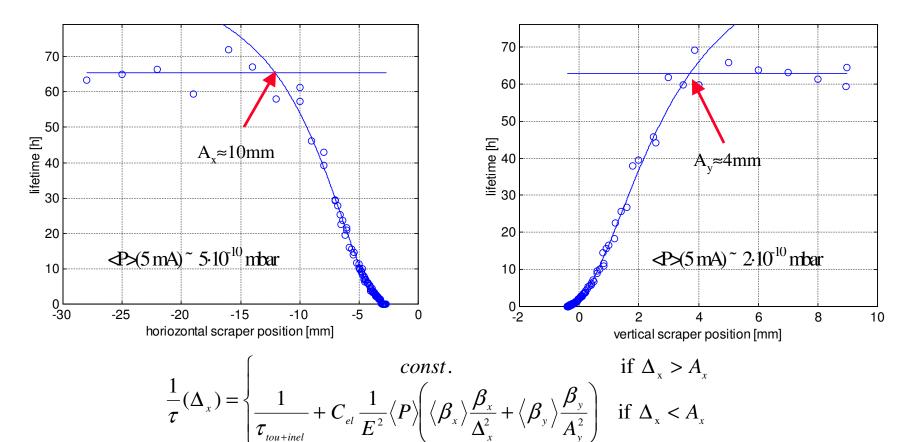




Transverse Acceptance and Gas Lifetime



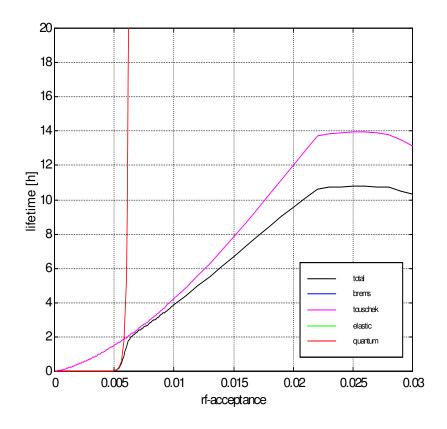
• move scraper into beam and record lifetime: acceptance, gas pressure



Assuming different distribution of the gas, i.e. higher pressure in the straight sections: **3*10**⁻¹⁰ **mbar** Desorption coefficient: 1.75*10⁻¹² mbar/mA

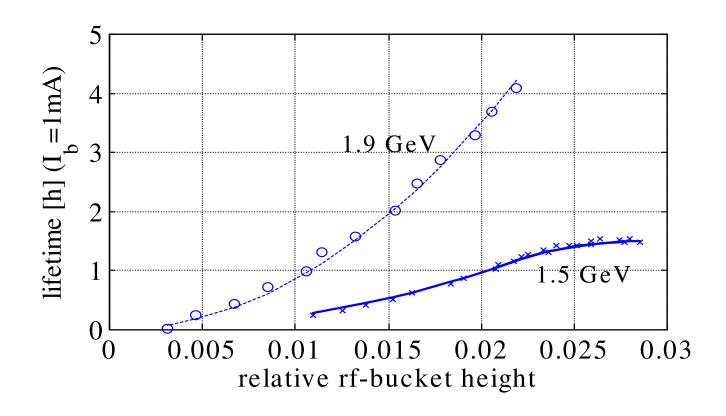
Dependency of Lifetime on Longitudinal Aperture

Theoretical results including bunch length change













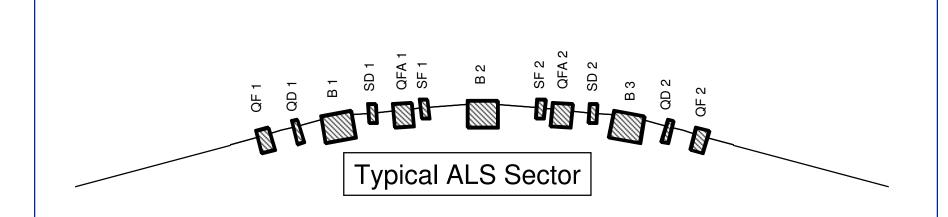
The stability of the motion of particles at large amplitudes is clearly important for a good performance of the storage ring.

- Lifetime
- Injection efficiency

Need to understand the beam dynamics

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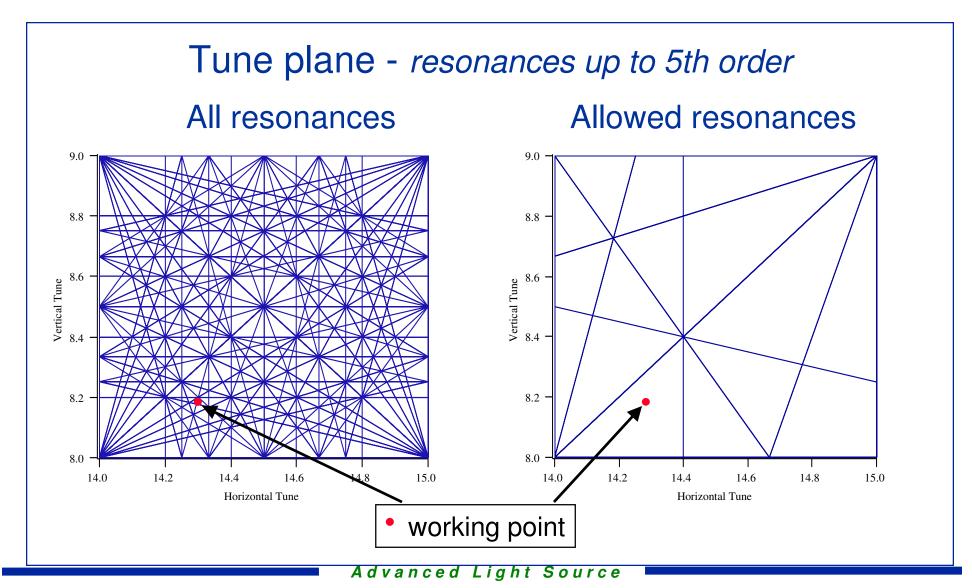
- ALS consists of 12 sectors
 - 12-fold periodicity \implies Suppression of resonances

$$m v_x + n v_y = 12 \times q$$

where m, n and q are integers

Benefits of Periodicity





Resonance Excitation



Resonances can lead to irregular and chaotic behavior for the orbits of particles which eventually will get lost by diffusion in the outer parts of the beam.

Rule of thumb => Avoid low order resonances

Unfortunately there is no simple way to forecast the real strength of a resonances without using a tracking code or through measurements

- => Tune scans
- => Frequency Map Analysis

Tune scan

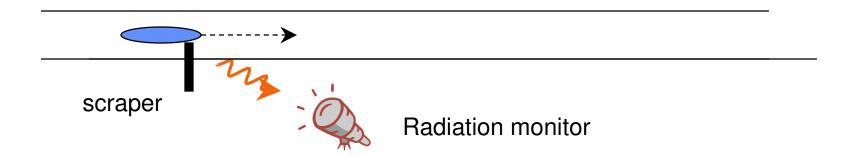


When resonances are present they may change the distribution of the beam at large amplitudes.

 In the case of a resonance island → particles may get trapped at large amplitudes

Technique:

By Introducing a scraper and a loss monitor



Scan the tunes and measure the change in the count rate

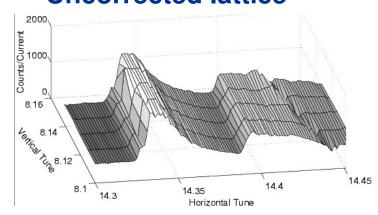
Developed by A. Temnykh (Proc. Of the IXth ALL-Union Meeting on Accelerators of Chaged Particles, Dubna, 1984, INP Peport No. INP 84-131

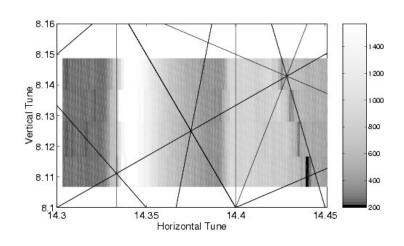
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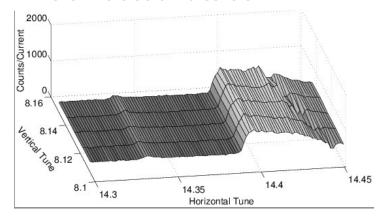


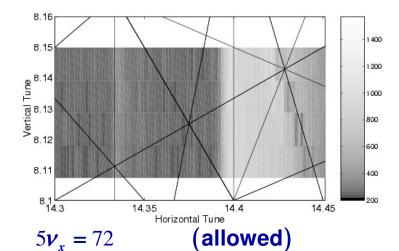
Uncorrected lattice





Corrected lattice





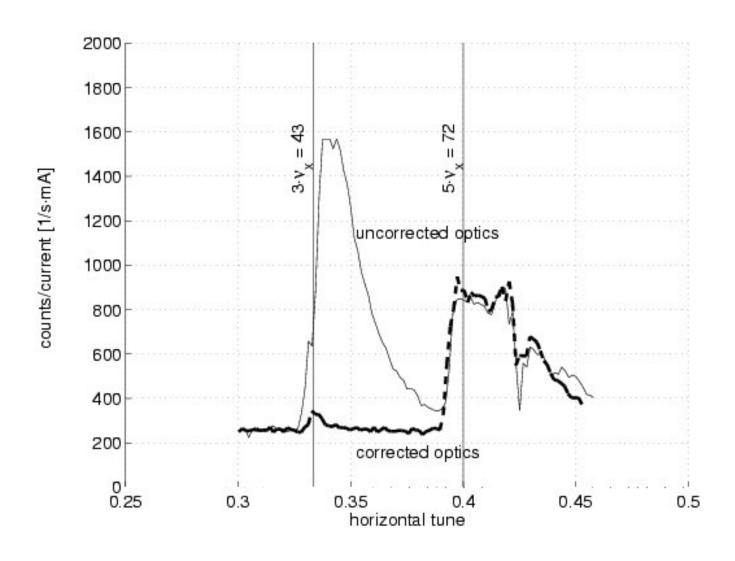
Three resonances are present:

$$3\nu_x = 43$$
 (unallowed)

Advanced Light $5v_{\text{ourch}} - v_{\text{ch}} = 37$ (unallowed)

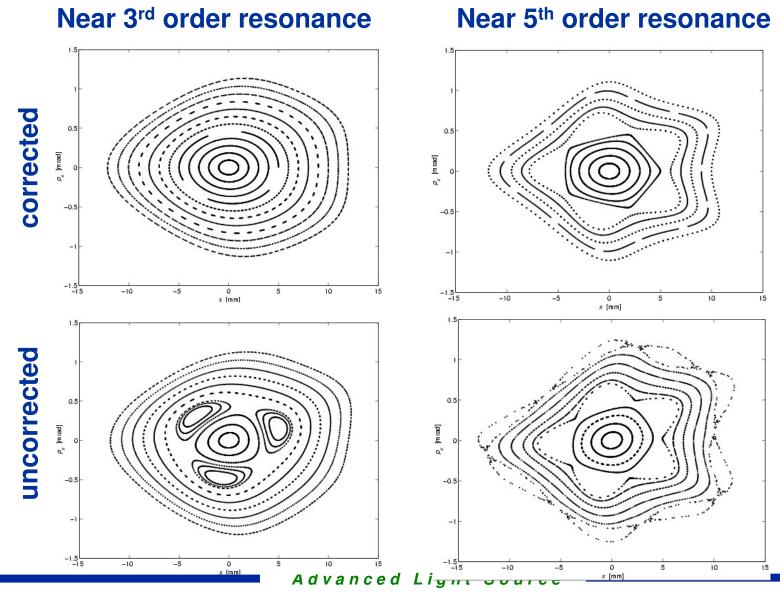


Large reduction in the unallowed resonances





Large reduction in the unallowed resonances







Profile measurement

0.2: 0.1 -0.1-0.2-

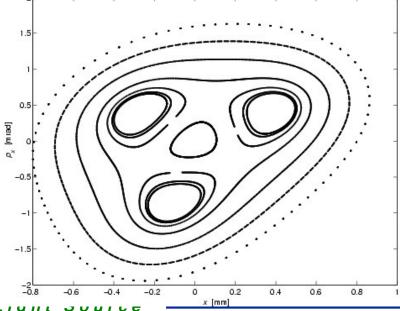
0.0

x [mm]

0.2

0.4

Horizontal phase space



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-0.4

-0.2

Tune scan summary



Advantages

Quickly and sensitively see excited resonances in the tails and core of the beam as a function of different tunes

Disadvantages

Probing different machines and not looking at the effect of resonances on one working point and at different amplitudes. This is what one really would like to see.



Tools and Techniques

The nonlinear dynamics in the ALS is determined by the sextupoles and the linear transport between them

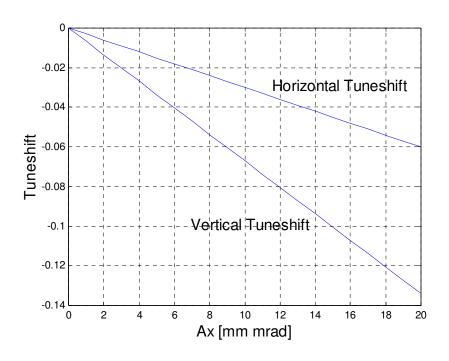
Tools and techniques for studying the dynamics

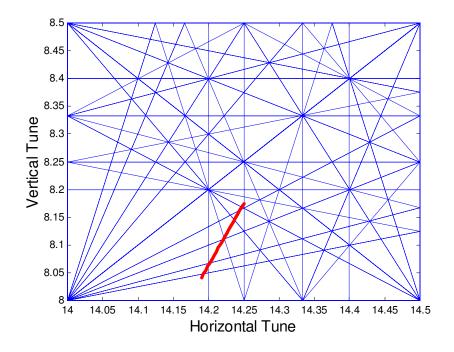
- Response matrix analysis (LOCO) to calibrate the linear model
- Symplectic integration and Frequency Map Analysis
 - Simulate the nonlinear dynamics and to get a global view of the dynamics (J. Laskar)
- Single turn kickers and BPMs, DCCT and RF scans
 - Test the model predictions
 - Model independent determination of the dynamics





Particle tune get shifted with amplitude





KAM Theorem (the basis of frequency map analysis)



According to the KAM theorem, in the phase space that is sufficiently close to an integrable conservative—system, many invariant tori will persist. Trajectories starting on one of these tori remain on it thereafter, executing quasiperiodic motion with a with a fixed frequency vector depending only on the torus.

Frequency Map Analysis



Developed by Jacques Laskar

The frequency analysis algorithm (NAFF) is a postprocesser for particle tracking data that numerically computes, over a finite time span, a frequency vector for any initial condition.

Frequency Map: Initial condition — Frequency vector

Based on the KAM theorem, frequency map analysis determines whether an orbit is regular or chaotically diffusing.

Regular orbits — Frequency vector remains fixed in time

Nonregular orbits — Frequency vector changes in time

Tunes and Diffusion Rates





+

FREQUENCY ANALYSIS POSTPROCESSOR

Track particle for **N** turns

Compute horizontal and vertical tunes v_{x1} and v_{y1}

Track particle for another **N** turns

Compute horizontal and vertical tunes v_{x2} and v_{y2}

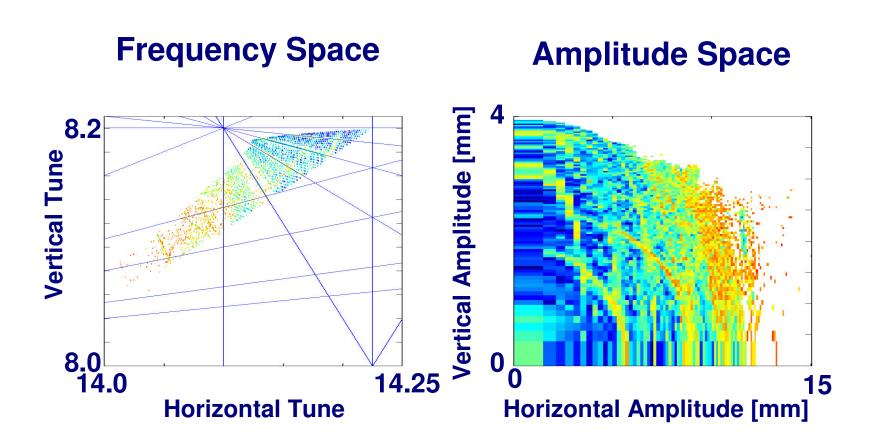
Compute diffusion rates

$$\frac{\partial v_x}{\partial \tau} \approx \frac{v_{x2} - v_{x1}}{N}$$

$$\frac{\partial V_y}{\partial \tau} \approx \frac{V_{y2} - V_{y1}}{N}$$

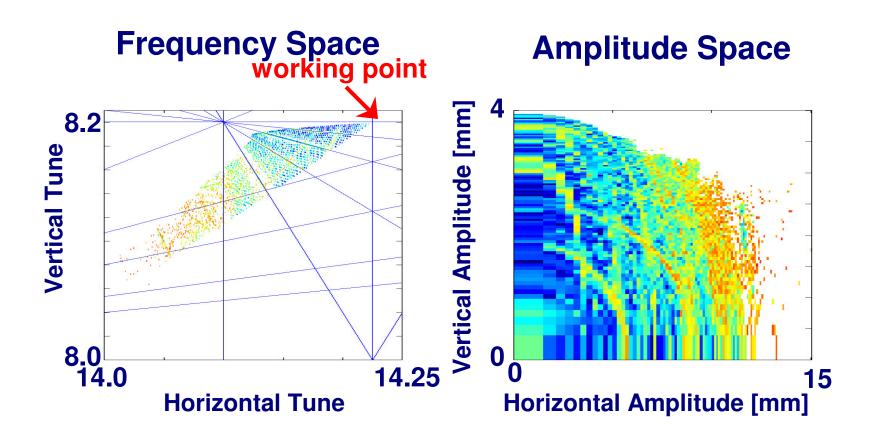






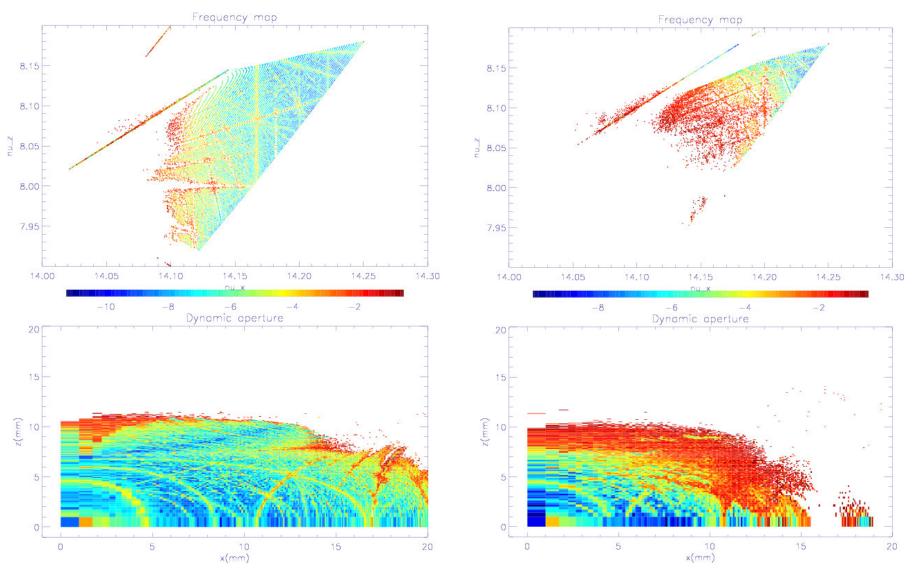








Ideal lattice vs. lattice with small errors



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Differences in dynamics

Linear lattice errors fundamentally change the beam dynamics

Ideal model:

- Dynamic aperture is large
- Chaotic zones at high amplitudes are small
- Particle loss is fast
- Particle loss due to allowed high order resonances

Calibrated model (linear errors):

- Dynamic aperture is smaller
- Large chaotic zones
- Particle loss is slow (diffusion)
- ◆ Particle loss due to unallowed lower order resonances

Is either of these models an accurate description of dynamics at high amplitudes in real ring? ⇒ test possible with Measured Frequency Maps

Experimental Procedure



Experimental Hardware

- ☐ horizontal + vertical single turn kicker
- □ 96 turn by turn monitors (1024 turns)

Experimental Procedure

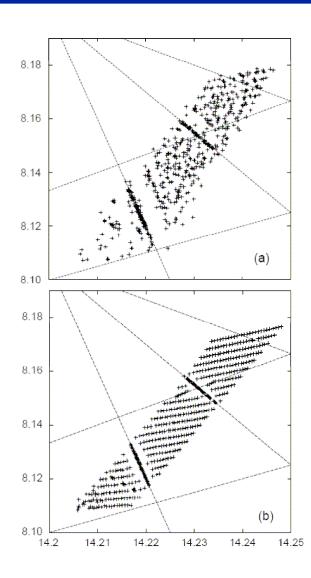
- □ Electron beam (single bunch or small bunch train) gets simultaneously a horizontal and a vertical kick
- ☐ Beam centroid oscillations are recorded turn by turn for 1024 turns
- □ Repeat with different initial conditions (hor. + vert. kick amplitude) → 400-600 total points per map

Data Analysis

□ turn by turn data is analyzed with frequency analysis post processor (NAFF) and results plotted in tune plane

Measured Frequency Map



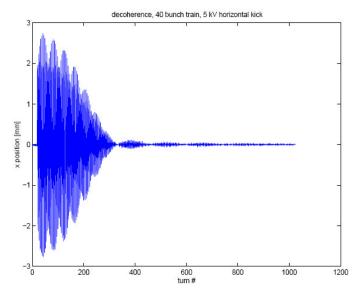


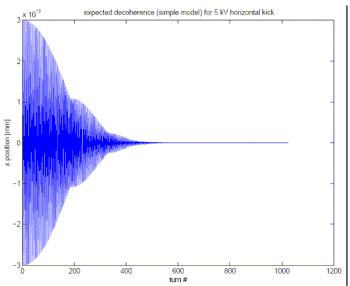
□ excellent agreement, using calibrated model (gradient errors), random skew errors, nominal sextupoles

Phys. Rev. Lett. 85, 3, (July 2000), pp.558-561

Fast Decoherence Problem for Experiment



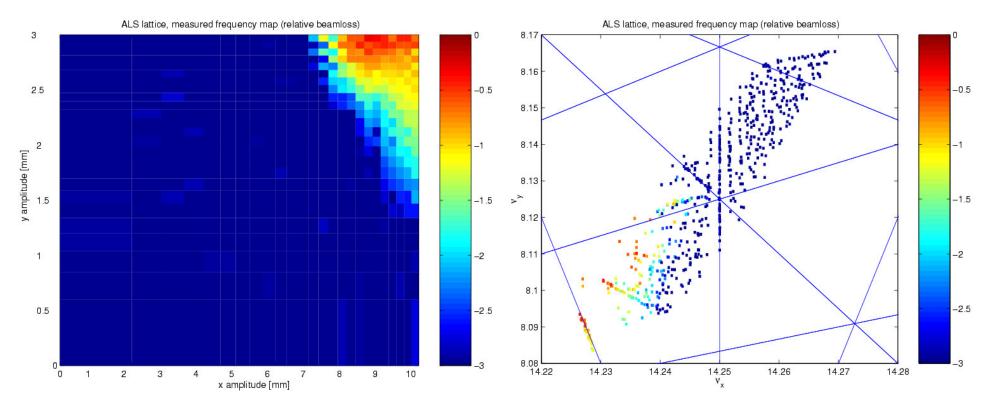




- Detuning with amplitude causes very fast decoherence for larger amplitudes
- Individual particles are still oscillating with same amplitude (radiation damping time >10k turns)
- Makes frequency analysis difficult
 - Small number of turns
 - Signal not quasiperiodic

Measured Frequency Map/Beam Loss





- ❖ Partial Beam Loss mostly if particles have to pass (radiation damping) through resonance intersection
- Isolated resonances not dangerous.

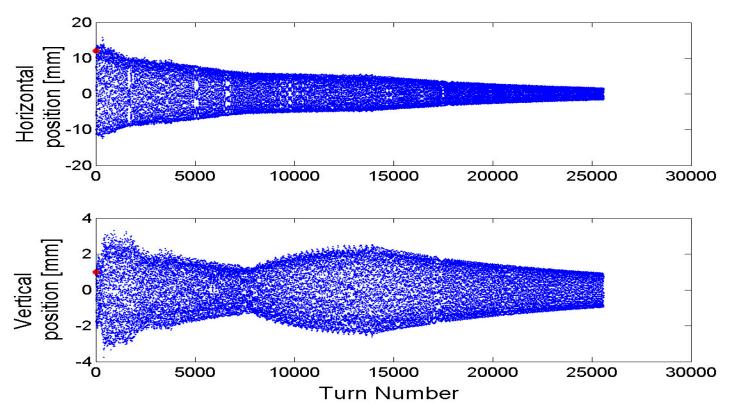
Side remark: Spectra contain more information than just fundamental frequencies – other resonance lines – resonance strength versus amplitude (see R. Bartolini, et al.).





Particle are lost in the vertical plane

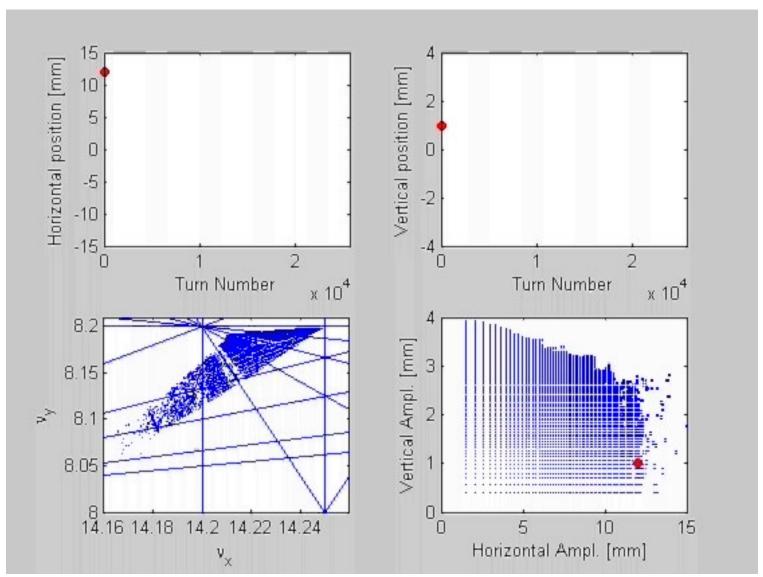
via nonlinear coupling and diffusion of the trajectory.



Example: Particle launched at 12 mm horizontally and 1 mm vertically and tracked with damping and synchrotron oscillations. (Simulated injection)



Tools and Techniques

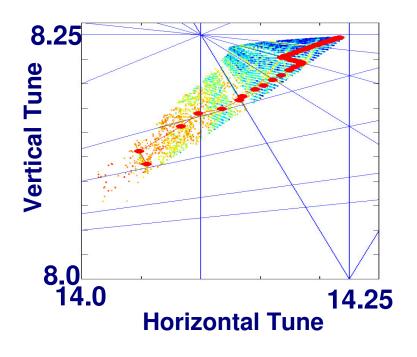


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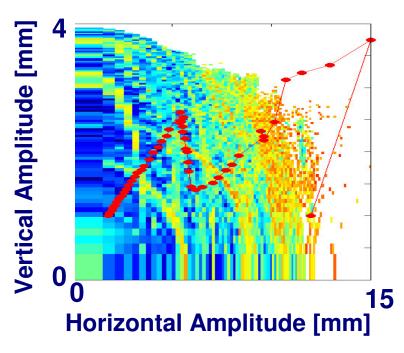
Frequency Map Analysis



Frequency Space

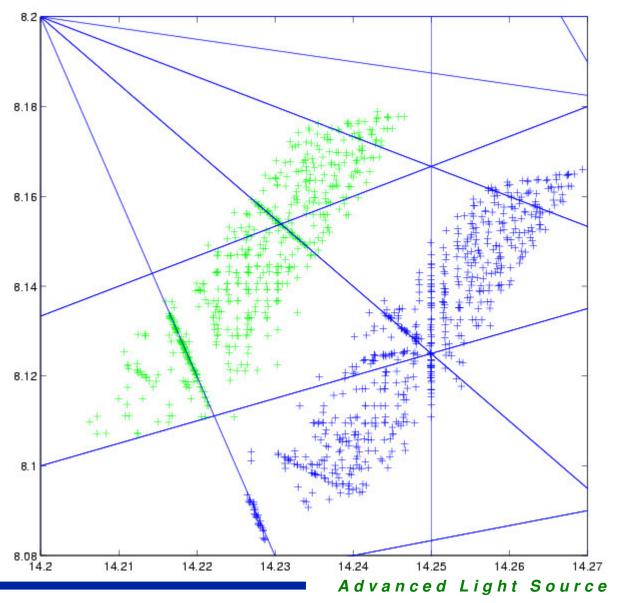


Amplitude Space





Model independent evaluation of dynamics



Frequency map analysis allows to model indepently evaluate how regular beam motion is



Off-energy dynamics: Touschek Lifetime

❖ Lifetime is crucial performance parameter for light sources ⇒ for 3rd generation light sources limit is Touschek lifetime ⇒ strong function of momentum aperture ε

$$\frac{1}{\tau_{tou}} \propto \frac{1}{E^3} \frac{I_{bunch}}{V_{bunch} \sigma_x^{'}} \frac{1}{\varepsilon^2} f(\varepsilon, \sigma_x^{'}, E)$$

- Momentum aperture ε is often limited by single particle dynamics
- ❖ 3rd generation light sources with their strong focusing to achieve small equilibrium emittances (small dispersion) and very strong sextupoles did originally not achieve their design momentum apertures of about 3%.





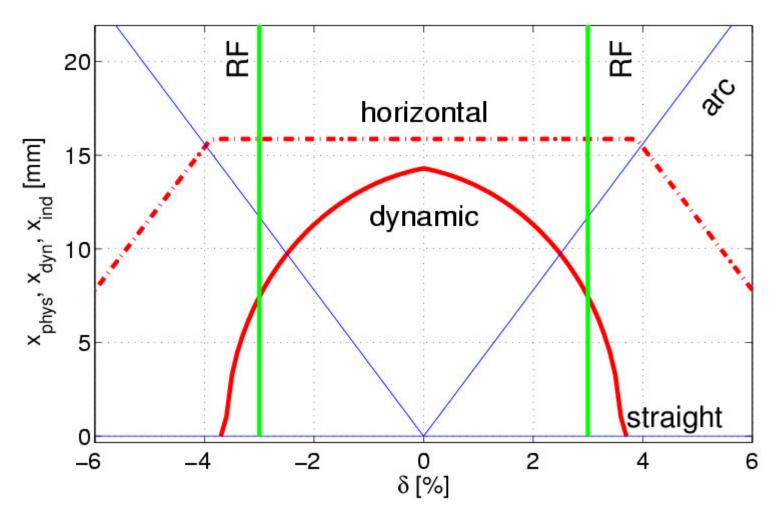
- Design momentum aperture for future light sources (like Soleil) 5-6% to achieve reasonable lifetimes
- Even using top-up (quasi continous) injection, lifetime is still an issue:
 - Radiation damage/safety
 - Injection transients are not fully transparent

Outline:

- What limits the momentum aperture?
- Practical Example: ALS
- Loss mechanism/Frequency Map Analysis (on energy ⇒ off energy)
- Measurements can serve as model independent debugging tool
- Impact of Coupling and Physical Apertures
- Summary

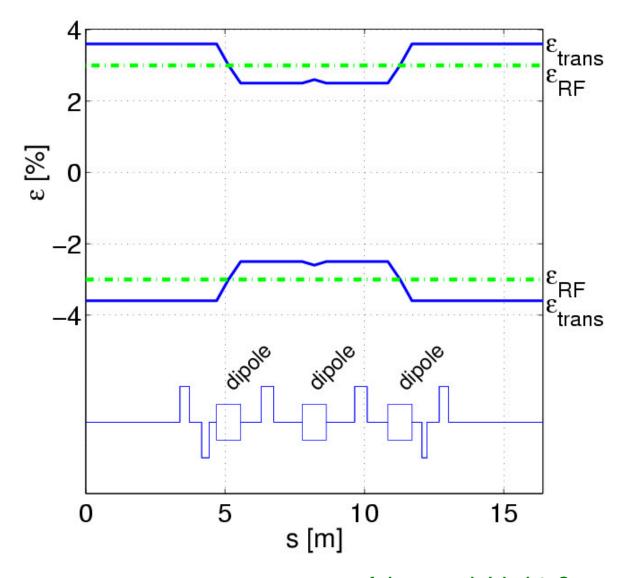
What determines the momentum aperture





Possible to quantitatively measure momentum aperture by scanning RF voltage

Longitudinal variation of momentum apertuferro



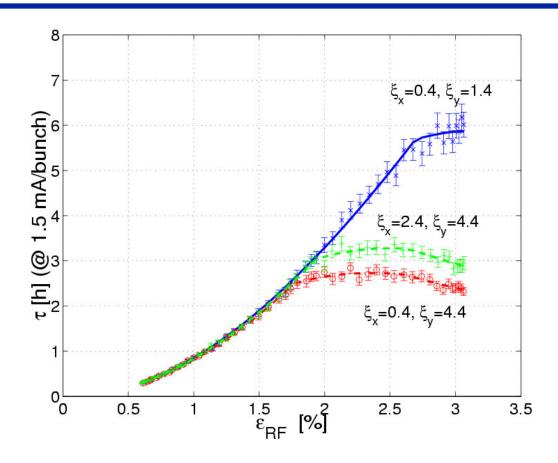
- Because of variation in H-function, momentum aperture will vary around the ring (depending on scattering location)
- Not necessarily symmetric for positive and negative momentum deviation (asymmetric bucket)

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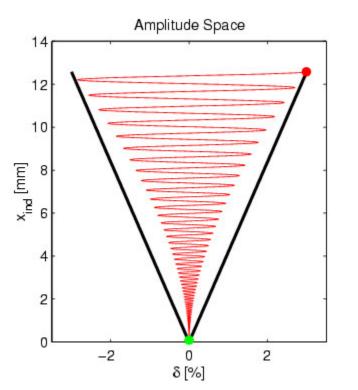
ALS example: RF amplitude scan

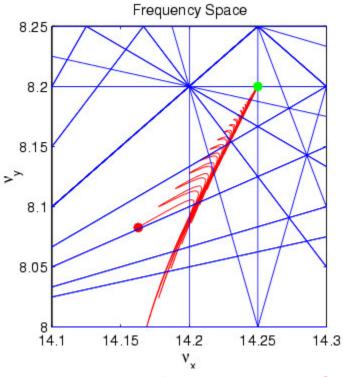


- Momentum aperture in ALS is clearly impacted by dynamics
- Sensitivity to chromaticity is at first surprisingly large (sextupole strength only different by a few percent).

Touschek Scattering – Tune Shift – Particle Loss



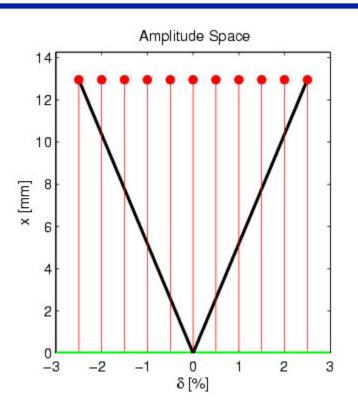


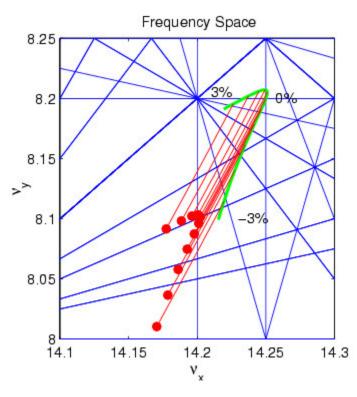


- ❖ Particle losing/gaining energy horiz. oscillation (dispersion/H-function) + long. Oscillation
- Particle changes tune
 - Synchrotron oscillations (chromaticity)
 - Radiation damping (detuning with amplitude and chromaticity)
- During damping process particle can encounter region in tune space where motion gets resonantly excited.

Measurement principle



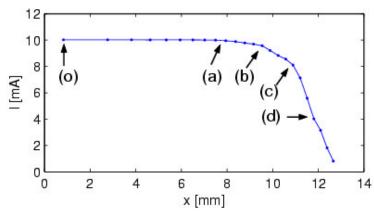


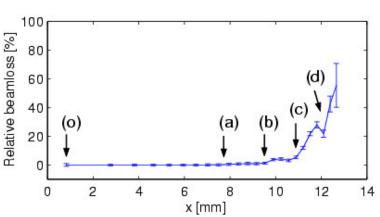


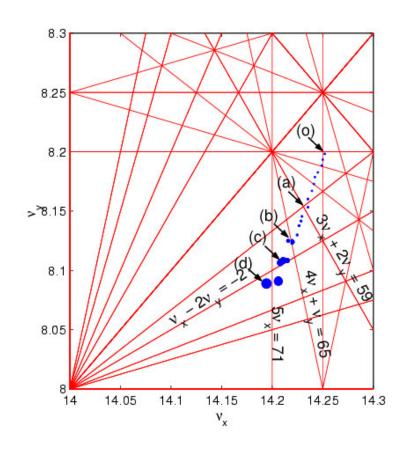
- ❖ Experimentally very difficult to exactly simulate Touschek scattering (simultanous kicks) – also difficult to measure tunes during synchrotron oscillations
 - Some positive results (Y. Papaphilippou et al.)
- Still possible to locate loss regions when scanning only transverse amplitude while keeping energy offset fixed

Measurement Detail









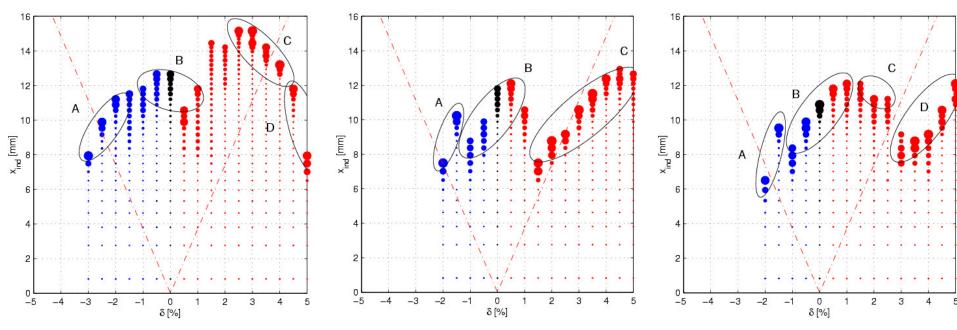
- Use single turn kicker to excite beam with increasing amplitude
- Use current monitor to record relative beam loss after kick
- Use turn-by-turn BPMs to record oscillation ferquencies

Aperture Scan for 3 Different Chromaticities

Small horiz. Chromaticity Small horiz. Small vert.

Large vert.

Large horiz. Large vert.



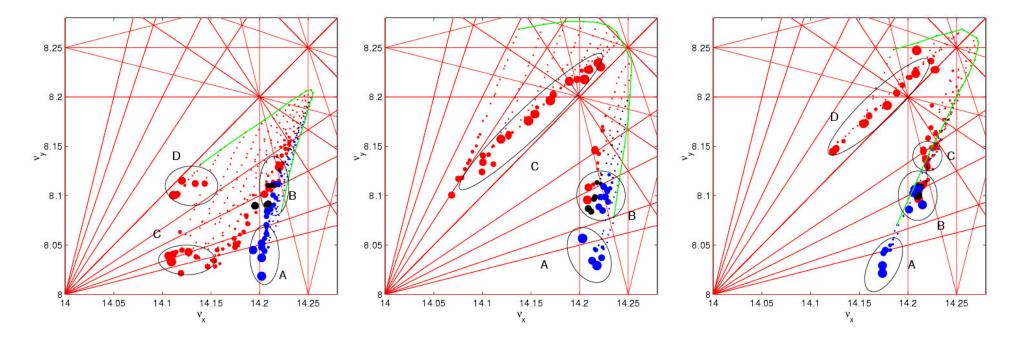
- ε > 3 % straight 2.65 % arcs
- ε = 2.6 % straight 1.75 % arcs
- ε = 2.6 % straight 1.9 % arcs

Aperture Scan for 3 Different Chromaticities

Small horiz. Chromaticity Small horiz. Small vert.

Large vert.

Large horiz. Large vert.



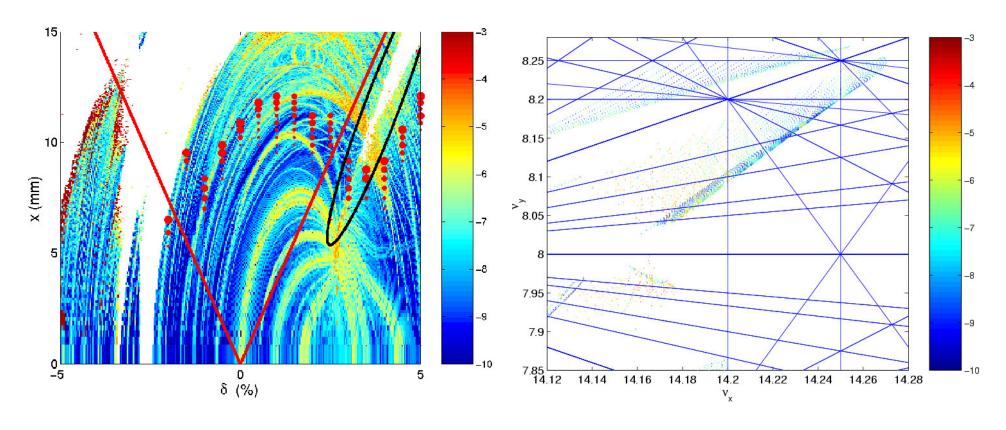
2.65 % arcs

 $\epsilon > 3$ % straight $\epsilon = 2.6$ % straight $\epsilon = 2.6$ % straight 1.75 % arcs

1.9 % arcs







Simulations reproduce shift of beam loss area caused by the coupling resonance to higher momentum deviations

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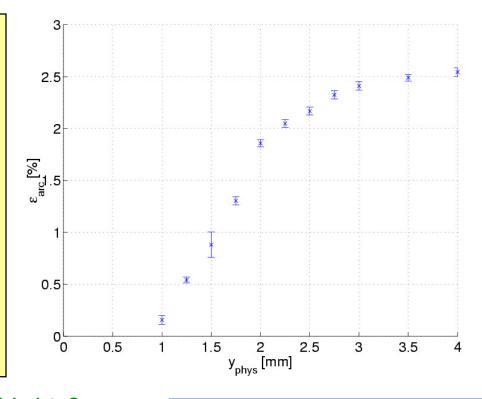
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Lifetime vs. Vertical Physical Aperture

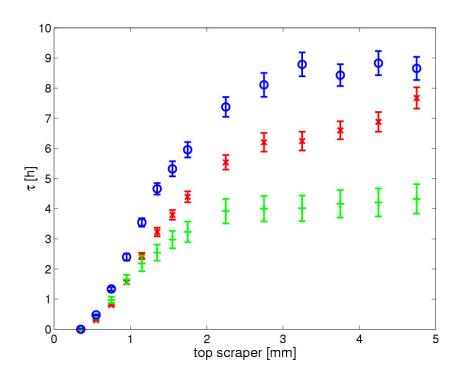


- $\ \ \, \ \ \,$ Found dynamic+momentum 'aperture' and (small) vertical physical aperture very closely linked for ALS momentum aperture collapses around 40-50 σ_y
- Since both are very important performance parameters studied link further:

- Performance (Brightness) of undulators/wigglers (both permanent magnet and SC) depends on magnetic gap
- Strong incentive to push physical aperture as low as possible
- Evolution at the ALS from 15 mm
 via 9 and 8 mm to now 5.5 mm –
 enabled by better understanding and optimization





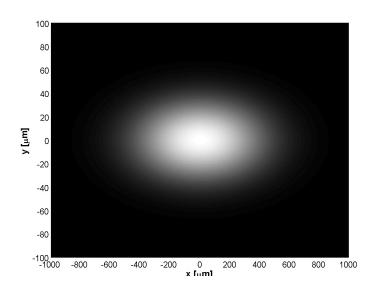


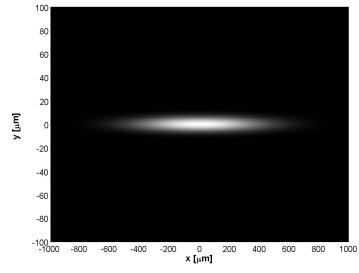
- Sensitivity of Touschek lifetime on vertical aperture depends on coupling
- High order coupling resonances scale similar to global/local coupling
- For given emittance ratio one can optimize coupling vs. vertical dispersion

Ultrasmall coupling allows small gaps



- Using LOCO and an optimized (based on simulations) skew quadrupole distribution with 18 skew quadrupole we achieved an emittance reduction from 150 pm (routine ALS operation) to about 5 pm (pictures on the right illustrate size reduction for insertion device straights)
- This was a world record at the time (now ATF about 4 pm) and about the NLC damping ring design value
- Correcting to those small coupling values and then using coupling free dispersion wave allows smaller vertical physical apertures.



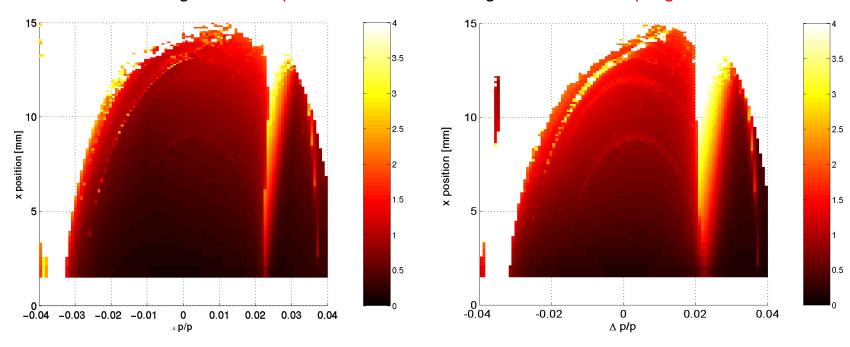




Simulation Results (Momentum Aperture – Gap)

Emittance increased using vertical dispersion wave ...

using excitation of coupling resonance



Tracking results are in good agreement with measured effects, i.e. case with dispersion wave has less yellow and orange areas than the one with excited coupling resonance, indicating less sensitivity to reduced vertical aperture

Summary



- ❖ Beam lifetime is determined by various scattering processes
- Can use scrapers, loss monitors, turn-by-turn BPMs, ... to study the details of lifetime limiting processes
- ❖ For many machines, the transverse single particle dynamics plays an important role for the injection efficiency (dynamic aperture) and (Touschek) lifetime (momentum aperture)
 - Measurement method using frequency analysis provides a very powerful model independent tool
 - Method has large potential in new light sources with many sextupole families
- Agreement between measurements and simulations are very good

Further Reading



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